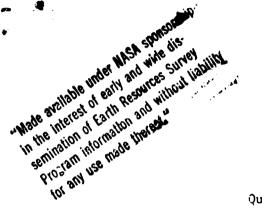
Quarterly Progress Report

Evaluation of SLAR and Thematic Mapper MSS Data for Forest Cover Mapping Using Computer-Aided Analysis Techniques

- Contract No. NAS 9-15889
- Reporting Period: June 1, 1980 August 31, 1980
- Submitted to: Exploratory Investigations Branch NASA Lyndon B. Johnson Space Center
- Prepared by: R. Hoffer, R. Latty, E. Dean, and D. Knowlton Laboratory for Applications of Remote Sensing Purdue University West Lafayette, Indiana 47906
- Technical Monitor: Mr. Norman Hatcher NASA Mail Code SF5 Exploratory Investigations Branch Houston, Texas 77058
- Principal Investigator: Dr. Roger M. Hoffer Ecosystems Program Leader LARS/Purdue University West Lafayette, Indiana 47906

LARS Contract Report: 083080



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NASA- CR-167791

E83⁻10148

Quarterly Progress Report

(E83-10148)EVALUATION OF SLAR AND THEMATICN83-16823MAPPER MSS DATA FOR FOREST COVER MAPPINGUSING COMPUTER-AIDED ANALYSIS TECHNIQUESUnclassQuarterly Progress Report, 1 Jun. - 31 Aug.Unclass1980 (Furdue Univ.)57 p HC AC4/MF A01G3/43

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> Original photography the purchased NASA STI FACILITY from EROS Data Conter Si II Falls, SD 57198

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I. ACTIVITIES OF THE PAST QUARTER

A. Data Collection

1. Radar Data Collection and Evaluation

The radar mission, Mission Number 424, was successfully flown on June 30, 1980. This was the first radar data to be obtained in support of the current project. The sensor used was the APQ-102 side-looking radar, and the aircraft platform was the WB-57F flown at an average altitude of approximately 60,200 feet MSL. Small scale color IR photography was also obtained of the study site as part of this mission.

The APQ-102 side-looking radar is a fully focused synthetic aperature radar imaging system. A horizontally polarized pulse of energy of 9600 MHz + 5 MHz (this wavelength band is commonly known as X-Band) was transmitted by the radar system, and the returning energy was recorded on separate holograms as horizontally (HH) and vertically (HV) polarized responses. These holograms were then processed through an optical correlator and the resulting images recorded on positive film, which was the format in which the data were provided by NASA to LARS.

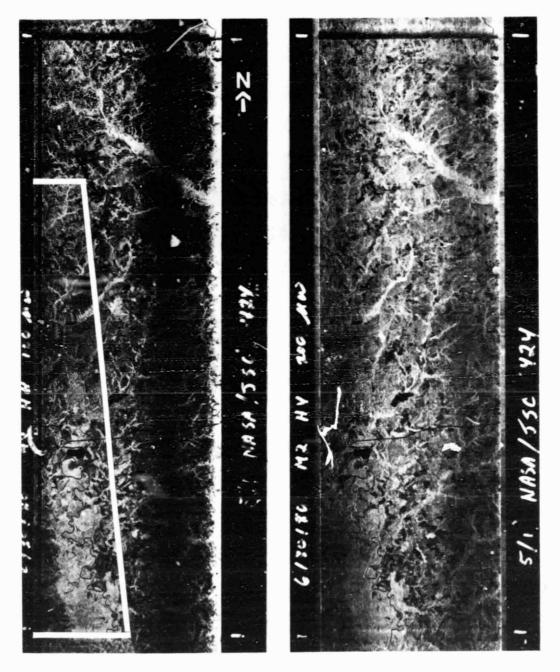
The positive-map film was received at LARS on August 8, 1980. Black and white negatives and positive prints were then made of the radar film for handling and pre-analysis purposes.

Visual comparison of the HH images and HV images indicates that there is a distinct dark band in the imagery which covers about 30 percent of the radar strip (see Figure 1). This band is very distinct on the HH images and is also quite noticeable on the HV images. Because the dark band falls on the test site for the Flight Line 2 data, the value of a detailed quantitative analysis of Flight Line 2 appears questionable (see Figure 2). However, the Flight Line 1 data looks reasonably good and the dark streak does not fall on the test site area, so this should provide a good data set for the quantitative analysis. Preliminary evaluation of the data indicates that various features on the HH and HV images seem to give different response levels, which provides promise for using this type of data to differentiate among various cover types and/or condition classes. This aspect of the data will be carefully studied.

The amount of sidelap due to the look-angle between Flight Lines 1 and 2 is negligible. This was surprising, since the flightline centers were defined to be only 5 n.mi. apart, but the swath width of the APQ-102 is 10 n.mi. Examination of the imagery indicated that the start (south end) of Flight Line 1 was exactly where it should have been, but apparently there was some drift as the aircraft flew up the flightline, resulting in a smaller portion of the test site being imaged at the northern end of the flightline (Figure 1). Flight Line 2 was flown 1-2 n.mi. to the east of the desired location, resulting in the lack of overlapping data. The slight amount of sidelap that does exist falls on the very edge of the data where the image quality is too poor to be of use. Since there is no useful sidelap in the data, analysis of forest cover as a function of look-angle (using the overlapping area of the two flight lines) cannot be pursued with this data set.

1

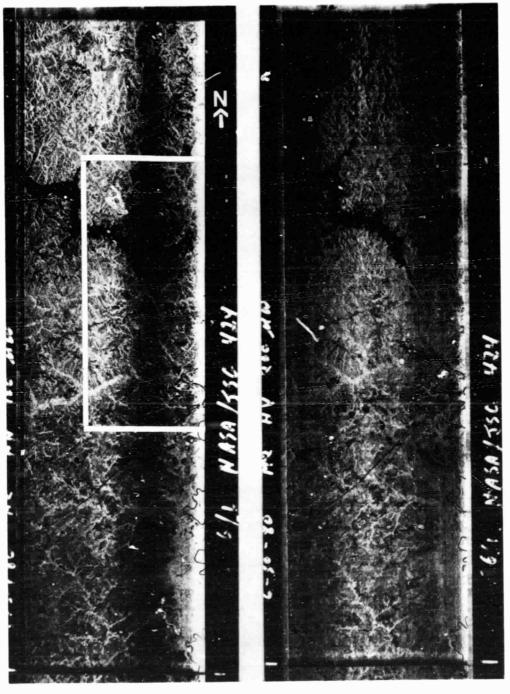
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HH

ΗV

Figure 1. Radar images of flight line 1 for the HH and HV polarizations. The corresponding area of the MSS data is outlined in white.



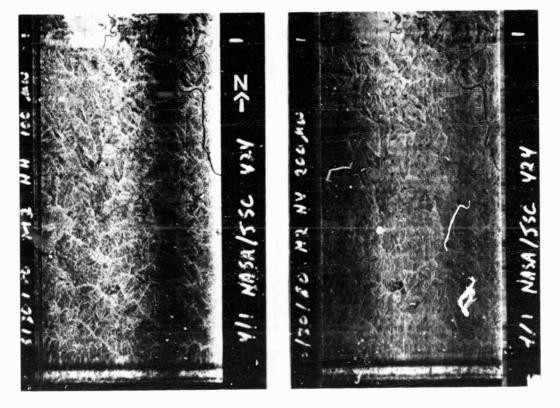
HH

ΗV

Figure 2. Radar images of flight line 2 for the HH and HV polarizations. The corresponding area of the MSS data is outlined in white.

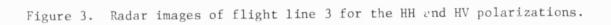
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HH

ΗV



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An estimation of the scale in the "along-track" and "across-track" directions indicates that there could be a significant difference between them. The scales were determined by measuring the distance between two points on the radar images and the same two points on USGS maps; two different measurements were taken for each direction and the averages computed. The approximate scale for the along-track direction is 1:361,000 and the across-track direction is 1:413,000. Normally on fully focused SAR systems the along-track and across-track scales are the same (Tomiyasu, 1978). This is because the length of the flight line over which the signals are combined is equivalent to the along-track length of the illuminated area at far range for any given pulse (Greer, 1975) . Because of this relationship many variables can influence both the along-track and across-track scales, and thus create significant differences between the scales even though the system is a fully focused SAR system. The SAR system is a phase-coherent system and the differences or phase errors can be attributed to system imperfections such as radar-platform velocity deviations, targets in motion, electromagnetic path length fluctuations, and electronic equipment instabilities (Tomiyasu, 1978) . Since spatial characteristics, such as resolution and swath width, of the radar system are based on the same properties used to determine the scale, the system parameters must be evaluated to make an accurate determination of the spatial characteristics of this data set.

2. Multispectral Scanner Data Collection

NASA Flight Mission #425 to obtain three flightlines of NS-001 MSS data and supporting aerial photography was successfully flown on July 2, 1980. A summary of the support data is shown in Table 1 along with characteristics of the camera equipment used.

The Flight Line 3 data quality was very good and virtually cloud-free. Flight Lines 1 and 2 both contained some cloud cover especially in the northern sections and near the city of Camden, South Carolina and over the adjacent Wateree Reservoir. Flight Line 1 over Camden and north of the city contained between 30% and 40% cloud cover while south of Camden the cover was only between 0% and 10%. The quality of Flight Line 2 was generally better than on Flight Line 1 and contained only between 10% and 20% cloud cover north of and over Wateree Reservoir.

Mission #425 was continued on July 3 in an attempt to collect scanner data over Flight Lines 1 and 2 under more favorable weather conditions. The weather was generally very hazy, however, and in some areas over 50% of the imagery was covered by either haze or cloud cover. This situation occurred both north of Camden on Flight Line 1 and north of the Wateree Reservoir on Flight Line 2.

3. Field Trip to the Study Site

A field trip to the study area was conducted by Ellen Dean from July 1 to July 3 for the purposes of obtaining ground information concurrent with NASA Flight Missions #424 and #425, and to become better acquainted with the study site and the characteristics and variability of cover types.

Flight #18 July 2, 1980 18:22:40 (time of flight)

Flightline	Run Time	Altitude(kft) MSL MGD	Line Miles	Ground Speed (mph)	Blackbody Temp (^O C)
1	6' 30"	21.4 20.9	35	299	14.8 (10) 36.7 (hi)
2	6' 20"	21.7 21.2	35	300	14.8 (10) 36.9 (hi)
3	3' 40"	21.4 20.9	22	297	14.9 (lo) 36.7 (hi)

Flight #19 July 3, 1980 14:52:35 (time of flight)

Flightli	ne	Run Time	<u>Altitu</u> <u>MSL</u>	<u>de(kft)</u> <u>MGD</u>	Line Miles	Gr	ound Speed (mph) Blac	kbody Temp (^O C)
1		6' 30"	21.5	21.0	35		285		15.7 (lo) 32.7 (hi)
2		6' 30"	21.6	21.1	35		270		15.4 (10) 32.7 (hi)
Film Type	Camera Type	Filter #1	Filter #2	Shutter Speed	Filter Factor	ASA	Focal Length	Forward Lap	Roll Number
S0397(C)	Zeiss	1A	36% T	1/250	2	160	6"	60%	22
S0193(CIR)	Zeiss	12	36% T	1/250	2	100	6"	60%	23

The first two days were spent in the field gathering reference information and color photographs of the various agricultural and forest cover types and conditions. These sites were located on aerial photographs from the previous NASA mission, Mission #399, noting the occurrence of any specific changes in the cover type. On July 3 a rental plane was flown over Flight Lines 1 and 2 at an altitude of approximately 900 feet above mean sea level and numerous aerial photographs were taken to be used in conjunction with other ancillary data to compare with data obtained from Missions #424 and #425. Subsequently these photographs were identified and labelled as to their corresponding positions on the CIR photos from Flight Mission #425.

To provide background information to use in the interpretation of the radar imagery, data on weather conditions was obtained for a period of one and two weeks prior to the flight missions (Table 2). This data was recorded at the Camden Weather Station, which is located in the center of Flight Line 1.

B. DATA ANALYSIS

1. Selection of Test Fields

A COMTAL Vision One/20 display device was used to aid in selection and photo interpretation of the test fields for the various spatial resolutions being investigated. Blocks of the geometrically and "radiometrically" adjusted imagery (see Quarterly Progress Report September 1, 1979 -November 30, 1979 for discussion) were used.

The first step involved designing a test sample grid such that the cover classes occurring at the various coordinates of the coarser resolutions could be identified using data of only one resolution displayed on the COMTAL. By designing the grid such that the set of pixels examined for the test pixel identification corresponded exactly with the set of pixels averaged in the resolution degradation program, the identifications made using the finest resolution data could be precisely mapped into the coarser resolutions. The spacing for the grid is thus determined by the smallest number for which all resolutions provide a common denominator. Since, for the across-track dimension, the resolutions are the average of 1, 2, 3, and 4 pixels then the spacing for the grid in the across-track dimension which will allow us to map exactly between resolutions is 12. Similarly for the along-track grid spacings; the pixels averaged together for each resolution are 1, 2, 3, and 5. Hence, the grid spacing must be a multiple of 30. The grid was generated by GRID.FTN (see Appendix B) for overlaying on the COMTAL image.

The COMTAL allows three different wavelength bands to be placed into separate image planes. These three planes can subsequently be assigned varying densities of red, green and blue colors, and overlaid to obtain a "truecolor" color composite image. This truecolor image was used, along with the ability of the COMTAL to magnify the image 1X, 2X or 4X, to accurately locate and identify the test fields. An example of this is shown in Figure 4 which displays one block of Flight Line 1 below Camden, South Carolina in magnification of 1X on which the Test Data Grid is overlaid. Figure 5 represents the central portion of the same scene at a 4X magnification.

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Date	Precipitation (inches)	<u>Temperatu</u> (high)	<u>ure (⁰F)</u> (low)	Relative Humidity (Kershaw Co.)
6/16	0.15			
6/17	0.15			
6/18	0.55			
6/19	none			
6/20	none			
6/21	none			
6/22	none			
6/23	trace	92	57	50%
6/24	0.7	90	68	-
6/25	1.37	90	68	-
6/26	trace	78	66	87%
6/27	none	82	62	58%
6/28	none	97	66	-
6/29	none	99	70	-
6/30	none	96	72	40%
7/1	none	98	64	41%
7/2	none	92	71	

Table 2. Weather Information from Camden, South Carolina



Figure 4: A COMTAL Vision/One image of Flight-line 1-S south of Camden, S.C. The image is overlaid with the grid used to locate and evaluate the test fields.

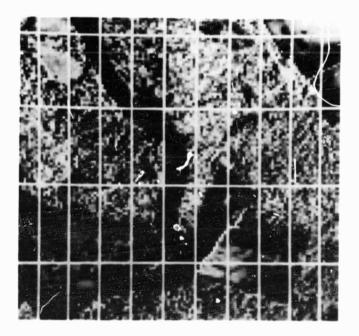


Figure 5: A magnification of a portion of the same image as shown in Figure 4. Magnification to this scale was used for most of the interpretation and identification of test fields.

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Identification of the cover type in the test fields at all resolutions on the COMTAL was done in comparison with photo interpretation of the CIR photos. Identification into various cover types followed the format as outlined in the Quarterly Progress Report of June 1, 1979 - August 31, 1979, except for an additional class of tupelo which was found to be both visually and spectrally separable. All test fields at the various resolutions were evaluated separately and any border test fields, i.e., pixels containing more than one cover type at a particular resolution, were excluded from the final data set. The COMTAL coordinates and the test point identifications were recorded for subsequent translation into MIST coordinates for each resolution. This work has been completed for Flight Line 1-S. Blocks in Flight Lines 1-N and 2-N are currently being analyzed.

2. Waveband Combination Evaluation

Much of the work conducted in waveband combination evaluation for this project is discussed in a paper prepared for presentation at the Fall Technical Convention of the American Society of Photogrammetry. A copy of this paper is included as Appendix A. Review of that article prior to reading the following text is suggested, as duplication is avoided wherever possible. However, there were several considerations and activities of the work that were not reported in the appended paper. The following discussions will focus primarily on these details of the analysis.

The <u>a priori</u> estimation of the probability of correct classification employing a measure of statistical difference between spectral classes relies heavily on: 1) the degree to which the group of class densities represent the distributions of spectral response vectors associated with each cover class (Swain, 1978) and 2) the degree to which the set of class densities is exhaustive of the range provided by the response vectors from the area to be classified (Wiersma and Landgrebe, 1979). If the class densities satisfy the above conditions, then statistical separability of the class densities should provide a fairly reliable estimate of percent correct classification.

The actual computation of transformed divergence, as well as the vast majority of other "separability" measures, involves only two class densities for each individual computation or value. Transformed divergence is thus a measure deemed appropriate for a two class case of equal a priori probability. A problem arises when such a measure is to be employed to provide an estimate of overall percent correct classification involving a multiple of spectral classes of unequal a priori probabilities. This problem is further compounded by the fact that subsets of these classes represent different cover classes. 1/ The averaged transformed divergence is given by:

$$TD_{ave} = \frac{1}{n} \sum_{k=1}^{n} TD_{k}$$
(1)

for n number of spectral class pairs.

^{1/} The need to provide estimates for only relative percent correct classifications for purposes of ranking possible waveband combinations does not alleviate the problem.

However, the relative frequency of each spectral class pair is assumed constant in such an approach. This is rarely the case.

An unweighted, arithmetic average of all TD-values will result in the separability of two infrequently occurring classes having equal impact on the percent correct classification estimate, as the separability of two common classes. Consider the following:

Given a probability space S, $s_{ij} \in S$, i = 1, ..., k - 1, j = i + 1, ..., kfor each j, where k = the total number of spectral classes. If each s_{ij} is considered the simultaneous occurrence of each spectral class of the pair (s_i and s_j), the occurrence of each being independent of the other, then the probability of the occurrence of the "spectral class pair" can be determined by:

$$W(s_{ij}) = P(s_{i}) P(s_{j}); \quad (s_{i} \cap s_{j}) = \emptyset$$
(2)

 $W(S_{ij})$ is a weight, distinct from the probability associated with an occurrence. To ease the complexity of indexing, it is assumed here that each cover class is represented by only one spectral class. The computations are easily extended into the case where the number of spectral classes in each cover class is greater than one. Then an unbiased estimator of averaged transformed divergence, corresponding more closely to probability of correct classification is given by:

$$TD_{ave} = \sum_{i=1}^{k-1} \sum_{j=i+1}^{k} W(s_{ij}) TD_{ij}$$
(3)

These probabilities should be treated with caution, as they are directed merely at extending the application of statistical distance as an estimator of probability of correct classification from the two class case to the multi-class case. The above presentation also assumes the availability of estimates of the $P(s_i)$ and $P(s_i)$. These are empirically derived using the relative frequency of each spectral class in each cover class and the relative frequency of each cover class. Computationally:

$$P(s_i) = P(s_i/C_{\alpha}) P(C_{\alpha}) \quad \alpha = 1, \dots, m$$
(4)

where: P(C) is given by the total number of pixels in the training data in cover class α divided by the total number of pixels from all cover classes in the training data.

 $P(s_i/C_a)$ is given by the total number of pixels in the training data spectral class s, which is a subset of C, divided by the total number of pixels in cover class $C_{\alpha} \cdot \frac{2}{\alpha}$

^{2/}As may well be apparent, the algebraic identify of these probability estimates provides a computational shortcut to the probabilities of interest.

While these frequencies are easily obtained, their use in providing unbiased estimations of the above probabilities is dependent on each observation being randomly selected. That is, the selection of each additional pixel in developing the training data is completely at random. While this is rarely the case, the extent to which this assumption is violated will erode the "goodness" of each P(s_i) and hence the resulting TD_{ave}. This has been used by some researchers as^{ij} the rationale for not weighting each observed TD_i and employing the unweighted arithmetic mean in the multiclass case. ^{ij} While this may well be warranted in many cases, it must be reconciled that weights are <u>always</u> employed. Where they are not computed and employed in the summation, they are merely assumed equal. Obviously,

$$\frac{1}{n}\sum_{k=1}^{n} TD_{k} = \sum_{k=1}^{n} \frac{1}{n} TD_{k}$$
(5)

The problem then becomes one of assuming some set of population parameters $(x_1, x_2, x_3, \ldots, x_k)$ where k is the number of spectral classes contained in the population and the x are the total number of pixels belonging to each ith spectral class.¹ The actual probabilities are then,

$$P(x_{i}) = x_{i} \begin{bmatrix} x \\ y = 1 \end{bmatrix}^{-1}$$
(6)

Then, for the weighted as opposed to the unweighted case:

$$E_{1} = \sum_{j=1}^{k} |\hat{P}(x_{j}) - P(x_{j})|$$
(7)

and

$$E_{2} = \sum_{i=1}^{k} \left| \frac{1}{k} - P(x_{i}) \right|$$
 (8)

where E_1 is the error for the weighted case and E_2 is the error for the unweighted case,

is
$$E_1 \geq E_2$$

This is the consideration which, in spite of not being testable, must be resolved before proceeding with any multiclass case employing averaged statistical distances. While an in-depth evaluation of this problem is beyond the scope of this study, the evaluation of waveband combinations employing the weighted average was considered imperative for complete treatment of this part of the study. Table 3 provides a rank ordering of channel combinations for each waveband combination level for the weighted mean TD-values.

The work in waveband combination evaluation prompted the development of several programs which were written to be compatible with LARSYS. These are listed in Appendix B with brief descriptions.

Among these was a program which computed average transform divergence over all spectral class pairs for each cover class pair and over all spectral class pairs for each cover class. The tables of these results are shown in Appendix C, and provide insight as to the dependency of waveband combination rank on cover class composition of the area to be classified. Such output will also assist individual users of diverse interest to select those waveband combinations most suited to their particular application. By selecting that waveband combination of maximum TD in cover classes with which they are concerned, the classifier can be "fine-tuned" according to the users needs. The disagreement between $\max(TD_{ave})$ by cover class, cover class pair, and overall cover classes is very common.

Separability by cover class pairs will also provide information on which cover classes may require additional spectral classes in order to reduce their variance. It will also give an estimate of the results to be expected in the omission-commission error matrix.

3. Spatial Resolution Evaluation

The development of test statistics have been completed for the southern half of the easternmost flight line (Flight Line 1-S) for all resolutions (i.e., 15x15, 30x30, 45x45 and 60x75 meter data sets). Prior to generating all of the statdecks for each resolution, an evaluation of the spectral classes for the 30 meter data was conducted by classifying the training fields.

As indicated in the paper included as Appendix A, statistics for each class density were provided by a supervised cluster approach. The linecolumn coordinates of supervised samples of each cover class were identified from the COMTAL Vision One/20. These coordinates were translated into MIST coordinates and a LARS-12 card deck was generated by CAGEN2 FORTRAN (see Appendix B). These were then sorted by cover class and separate cluster analyses were run for each cover class. The individual statistics decks were merged, providing 32 spectral classes for 12 cover classes. Table 4 contains the resulting class parameters by spectral class, by cover class.

Separability indicated that these class densities were on the average, very separable and that acceptable classification accuracies could be expected. However, in order for class densities to provide high classification accuracies the classes must be:

- representative of the distribution of observations of the same class,
- 2) separable or distinguishable among all other classes,
- 3) exhaustive of the sample space from which observations are drawn.

Table 3. Rank Ordering of Best Seven Channel Combinations for each Channel Combination level (ordering criterion is Average Transformed Divergence over all spectral class pairs).

1	2	3	4	5	6
6	3,4	3,4,5	1,3,4,5	1,2,3,5,6	1,2,3,4,5,6
3	3,5	3,4,6	3,4,5,6	1,2,3,4,6	1,2,3,5,6,7
4	2,4	3,5,6	1,3,4,6	1,2,3,4,5	1,2,3,4,6,7
5	4,6	2,4,5	2,3,4,6	1,3,4,5,6	1,2,3,4,5,7
1	3,6	1,3,4	2,3,4,5	2,3,4,5,6	1,2,4,5,6,7
2	2,5	2,4,6	2,3,5,6	1,2,4,5,7	2,3,4,5,6,7
7	5,6	2,5,6	2,4,5,6	1,2,4,5,6	1,3,4,5,6,7

Note:	Channel	1	=	0.45		0.52	μm
	Channel	2	=	0.52	-	0.60	μm
	Channel	3	=	0.63	-	0.69	μm
	Channel	4	=	0.76	-	0.90	μm
	Channel	5	=	1.00	-	1.30	μm
	Channel	6	=	1.55	-	1.75	μm
	Channel	7	=	10.4	-	12.5	μm

Table 4 . Summary of Statdeck Containing 32 Spectral Classes.*

14510 4	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	7
SOILI	154.87	177.14	189.70	181.14	188.11	189.22	143.31
	243.34	635.95	705.00	320.86	308.40	513.50	757.91
SOILS	128.42	125.67	128.85	135.62	144.49	144.83	139.44
	38.26	194.42	249.09	223.42	158.03	158.41	1162.87
SOTL3	$111.10 \\ 105.86$	95.43 235.72	92.80 348.18	99.29 361.95	$109.41 \\ 331.33$	106.21	135.06 734.38
PASTI	93.84	74.46	62.05	118.41	122.58	91.51	137.99
	24.88	41.55	92.69	259.57	187.63	90.66	432.61
PAST2	87.89	65.24	44.09	155.37	135.89	68.69	86.19
	22.39	38.95	24.31	140.19	93.50	68.85	74.75
PAST3	85.36	61.38	42.37	119.42	106.93	57.08	80.27
	20.05	27.50	40.48	258.94	140.35	57.77	122.54
PAST4	96.11 9.05	72.36	57.77 21.87	38.39 103.32	31.09 112.83	22.08 77.18	45.94 322.49
CROP1	117.65 42.54	$111.12 \\ 130.55$	100.67 309.75	172.25 203.03	161.50 140.88	119.58 229.37	103.02 221.09
CROPS	100.77 5.80	76.21 16.76	52.34 22.41	$ < 10.17 \\ 176.97 $	160.62 39.00	68.76 40.72	82.34 40.46
CROP3	99.82	82.30	71.21	118.67	117.97	91.50	137.56
	37.79	37.85	70.73	115.25	118.15	203.40	269.31
CP7P4	96.03 5.16	76.84 30.63	58.40 45.41	150.22 199.39	$127.02 \\ 141.36$	64.76 70.29	97.05 194.62
PINEI	92.26 3.11	69.70 5.35	54.05 13.48	113.46 81.46	$115.17 \\ 55.40$	71.85 50.93	116.23 298.47
PINES	94.75	57.90	48.67	118 .7 9	112.27	59.60	83.64
	15.59	8.73	5.99	104.99	83.46	40.22	73.18
PIHOL	91.69	69.46	55.44	109.79	110.61	70.28	127.44
	14.58	8.39	11.86	64.(6	46.92	28.63	379.38
рІнр5	94.31	65.79	46.98	112.63	105.95	53. 95	84.25
	6.()4	7.81	7.09	119.94	85.44	29.96	54.55
HDWD1	84.36 9.19	51.83 19.05	42.03 14.24	140.62 228.86	125.34	63.50 67.09	24.96 98.88
HDW02	91.78	70.90	59.56	99.01	101.23	76.15	125.33
	24.90	47.12	121.63	010.36	911.00	679.65	909.75
SGHD1	→1.42 7.13	67.31 9.40	44.23 5.47	175.67 55.54	$150.73 \\ 38.43$	71.57 29.82	84.74 55.83
SGHD2	86.10	51.11	40.46	155.12	133•75	63.66	81.08
	32.01	20.54	5.09	54.63	29•75	17.06	80.84
SGHD3	91.52 13.22	64.64 9.93	41.91 5.45	131.63 126.96	112.29	56.05 16.65	69.85 34.31
TUPE1	84.63	61.26	41.99	134.63	119.80	60.42	80,56
	4.51	12.07	15.19	366.89	253.77	69.31	146.03
TUPE2	78.38 3.70	50.18 15.81	38.94 23.85	$44.15 \\ 168.05$	45.85 385.93	35.99 304.10	112.04 809.13
SYCAl	87.53	66.20	50.40	123.40	124.13	82.87	116.73
	2.93	4.89	13.40	368.97	204.27	11.41	105.64
SYCAR	84.40	60.05	39.70	130.50	115.20	56.95	80.05
	2.15	4.58	7.81	294.47	167.96	28.58	35.84

Table 4 . Summary of Statdeck Containing 32 Spectral Classes (cont'd.).

	1	2	3	4	5	<u>6</u>	<u>7</u>
CCUT1	99.76 47.58	82.77 106.86	83.37 286.95	91.37 384.24	102.79 297.92	102.92 423.73	136.91 167.45
CCUT2	84.78 17.53	63.53 36.59	44.63 43.53	141.22 238.84	128.27 127.66	69.31 81.24	93.55 197.84
MVEG1	102.64 22.73	79.12 73.10	$55.10 \\ 174.96$	$110.00 \\ 58.54$	123.25 51.46	89.91 102.11	123.56 204.00
MVEG2	$100.76 \\ 8.90$	76.83 20.02	52.67 14.55	123.72 173.99	112.42 118.27	64.49 65.70	$80.16 \\ 113.35$
TUWA1	172.62 107.95	195.02 279.18	139.18 79.42	55.29 94.48	37.92 120.65	27.02	76.42 28.94
VEGE1	126.03 162.80	114.84 502.68	88.24 336.21	104.05 242.38	95.88 392.74	63.05 204.28	90.47 115.30
VEWA1	$107.63 \\ 19.90$	82.53 36.55	55.08 27.34	61.83 119.81	57.93 111.52	42.91 59.06	88.04 29.35
WATR1	$107.08 \\ 43.52$	79.41 123.32	52.51 31.19	39.08 13.04	$33.05 \\ 17.75$	24.97 14.22	71.62 143.33

*Within each spectral class, the upper element is the mean and the lower is the variance.

Channel Number	Band
1	0.45 - 0.52 μm
2	0.52 - 0.60 µm
3	0.63 - 0.69 µm
4	0.76 - 0.90 µm
5	1.00 - 1.30 µm
6	1.55 - 1.75 μm
7	10.4 - 12.50 µm

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	No. of	%															
	Pts.	Correct	Soil	Past	Crop	<u>Pine</u>	Pihd	Hdwd	Sghd	Tupe	<u>Syca</u>	<u>Ccut</u>	Mveg	Tuwa	Mveg	Vewa	<u>Watr</u>
Soil	1946	88.6	1724	0	22	1	2	0	0	0	0	178	9	1	6	2	1
Past	987	24.7	60	244	520	1	0	144	3	0	0	6	6	0	3	0	0
Crop	1445	98.1	6	5	1417	2	1	0	1	0	0	11	1	0	1	0	. 0
Pine	805	81.4	0	7	0	655	125	14	0	0	0	0	4	0	0	0	0
Pihd	314	89.8	0	0	0	26	282	2	1	0	0	0	2	0	1	0	0
Hdwd	3997	5.1	0	637	1	1	11	202	2301	691	104	41	7	0	0	1	0
Sghd	2242	94.0	0	61	2	0	1	52	2107	9	0	7	1	0	0	2	0
Tupe	350	0.0	0	186	52	0	0	101	4	0	0	0	7	0	0	0	0
Syca	35	0.0	0	11	3	0	0	0	20	0	0	0	1	0	0	0	0
Ccut	4277	17.9	234	2460	40	156	4	508	33	3	28	765	32	0	2	11	1
Mveg	294	98.0	3	0	0	3	0	0	0	0	0	0	288	0	0	0	0
Tuwa	124	99.2	0	0	0	0	0	0	0	0	0	0	0	123	1	0	0
Mveg	66	100.0	0	0	0	0	0	0	0	0	0	0	0	0	66	0	0
Vewa	39	97.4	0	0	0	0	0	0	0	0	0	0	0	0	1	38	0
Watr	232	97.0	0	7	0	0	0	0	0	0	0	0	0	0	0	0	225

Table 5. Classification Performance Evaluation from Classification of Training Data with 32 Class Training Statistics.

Overall Classification Accuracy (8136/17153) = 47.4%

Table 6 . Summary of Statdeck Containing 37 Spectral Classes.*

	1	2	3	4	<u>5</u>	<u>_6</u>	<u>7</u>
SOTL1	154.87 243.34	177.14 635.95	199.70 705.00	191.14 320.86	$188.11 \\ 308.40$	189.22 513.50	143.31 767.91
SOILS	128.42 83.26	125.67 194.42	128.85 240.09	135.62 223.42	144.49 158.03	144.93 158.41	139.44 1152.87
SOIL3	$111.10 \\ 105.86$	95.03 235.72	92.80 308 . 13	99.29 361.95	109.41 331.33	106.21	135.06 734.38
PAST1	$107.48 \\ 9.79$	93.05 29.30	81.10 74.74	148.14 151.33	162.16 87.59	131.79 83.29	197.08 283.63
PAST2	104.65 4.75	85.95 9.49	62.46 17.70	188.67 116.83	176.23 34.90	102.77 51.15	145.38 138.17
PAST3	$104.30 \\ 19.73$	85•V4 22•34	55 . 93	141.03 162.09	$148.91 \\ 97.33$	108.70 68.28	154.41 196.43
PAST4	99.52 8.07	39.96 13.68	58.73 17.95)71.73 222.32	154.58 59.78	64.27 35.41	$115.33 \\ 58.16$
PAST5	97.60 5.56	73.76 7.50	51.20 7.15	165.09 46.32	$135.90 \\ 30.41$	63.37 25.35	87.51 55.28
CROP1	117.65 42.54	$111.12 \\ 139.55$	100.67 309.76	172.25 203.03	161.50 140.88	119.50 229.87	20.601 20.601
CROP2	$100.77 \\ 5.80$	76.21 16.76	52.34 22.41	$210.17 \\ 176.97$	160.62 39.00	08.76 40.72	82.34 40.46
CROP3	99.82 37.79	32.30 37.85	71.21 70.78	118.67 115.25	117.97 118.15	91.60 203.40	137.56 268.31
CROP4	96.08 5.16	76.84 30.63	58.45 45.40	150.22 199.89	127.02 141.36	64.76 70.29	97.05 194.62
PINE1	92.26 3.11	69.76 6.35	54.05 13.40	113.45 81.46	$115.17\\65.40$	71.80 50.93	116.23 288.47
PINES	94.75 13.59	57.90 8.73	48.67 5.99	118.79 104.89	112.27 83.46	59.60 40.22	83.64 73.18
bIHD1	91.69 14.58	69.46 8.39	55.44 11.85	109.79 54.06	110.61 45.92	71.28 28.53	127.44 379.38
PIHDS	$94.31 \\ 6.04$	65.79 7.81	45.93 7.09	$112.63 \\ 119.94$	105.95 35.44	53.95 29.96	84.25 54.55
HDMD1	92.12 2.48	66.21 4.29	43.92 2.64	161.01 38.25	138.32 20.72	63.29 15.45	78.90 30.02
HD⊮DS	91.45 4.73	66.07 11.20	43.94 5.93	146.15 30.91	$127.10 \\ 16.15$	61.37 17.43	77.05 43.73
нрырз	34.52 3.75	58.21 7.59	38.78 5.89	$124.69 \\ -36.81$	108.22	52.82 10.90	72.92 19.29
SGHD1	91.42 7.13	$67.31 \\ 9.40$	44.23 5.47	175.67 55.54	$150.73 \\ 38.43$	71.57 29.82	84.74 55.83
SGHD2	86.10 32.01	61.11 20.54	40.45 6.09	155.12 54.63	133.78 29.75	63.65 17.06	81.08 80.84
SGHD3	91.52 13.22	64.64 9.93	41.01 5.4%	131.63 125.96	112.29 92.78	56.05 15.65	60.85 34.31
TUPE1	95.44 7.53	80.55 12.71	51.29 3.64	183.49 66.36	155.89 30.81	77.28 10.74	80.27 97.30
TUPES	95.67 7.47	80.57 12.79	51.88 4.47	$154.41 \\ 45.11$	141.59 36.50	74.01 12.20	81.98 37.88

	<u>1</u>	2	3	4	<u>5</u>	6	7
TUPE3	82.83 8.41	72.87 3.40	46.51 0.89	$124.39 \\ 11.67$	109.04 6.59	60.90 1.53	79.67 22.23
SYCA1	87.53	66.20	50.40	123.40	124.13	82.87	116.73
	2.98	4.89	13.41	368.97	204.27	11.41	105.64
SYCA2	34.49 2.15	4.58	39.70 7.80	130.50 294.47	115.20 167.96	56.95 28.58	30.05 35.84
CCUT1	101.66	93.29	73.24	121.39	135.02	112.71	189.76
	39.09	50.16	145.27	163.30	73.32	123.54	463.75
CCUTS	96.86	76.45	64.94	107.61	114.36	91.23	137.69
	17.11	35.73	117.13	191.87	140.05	98.60	198.27
CCUT3	91.66 7.20	70.97 11.70	50.25 19.19	142.64 275.54	$131.36 \\ 110.55$	77.78 44.09	100.85 132.54
CCUT4	91.17	66.86	52.46	83.56	83.20	62.04	98.73
	19.28	26.99	75.15	31.60	325.53	164.53	300.15
MVEG1	102.64	79.12 73.10	65.10 174.96	$110.00 \\ 58.84$	123.25 51.46	89.91 102.11	123.56 204.00
MVEG2	100.76	76.83	52.67	123.72	112.42	64.49	80.16
	8,90	20.02	14.56	173.99	118.27	66.70	113.35
TUWA1	172.62	195.82	139 . 18	55.29	37.92	27.12	76.42
	107.95	279.18	79 . 42	94.48	120.65	95.07	28.94
VEGEL	126.08	114.84	88.24	104.06	95.88	63.05	90.47
	152.80	502.60	336.20	242.38	392.74	204.28	115.30
VFWA1	$107.63 \\ 19.90$	82.53 36.85	55.08 27.39	$61.83 \\ 119.81$	57.93 111.52	42.91 59.06	88.04 29.35
WATRI	107.08 43.52	78.41 123.32	52.51 31.19	$39.08 \\ 13.04$	33.05 17.75	24.97 14.22	71.62 143.33

*Within each spectral class, the upper element is the mean and the lower is the variance.

Channel Number	Band
1	0.45 - 0.52
2	0.52 - 0.60
3	0.63 - 0.69
4	0.76 - 0.90
5	1.00 - 1.30
6	1.55 - 1.75
7	10.4 - 12.50

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Table 6. Summary of Statdeck Containing 37 Spectral Classes (cont'd.).

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Classification Performance Evaluation from Classification of Training Data with 37 Class Training Statistics. Table 7.

Watr	1	0	0	0	0	0	0	0	0	н	0	0	0	0	232
Vewa	2	0	0	0	0	0	2	0	0	4	0	0	0	38	0
Vege	9	0	1	0	Ч	0	0	0	0	ы	0	Ч	66	ы	0
Tuwa	, - 1	0	0	0	0	0	0	0	0	0	0	123	0	0	0
Mveg	7	0	Н	4	2	4	⊢ 1	2		15	287	0	0	0	0
Ccut	46	29	S	19	2	75	16	0	ε	3693	7	0	0	0	0
Syca	0	0	0	0	0	37		0	0	25	0	0	0	0	0
Tupe	0	0	0	0	0	2	9	346	11	39	0	0	0	0	0
Sghd	0	1	Ч	0	0	357	1907	0	20	22	0	0	0	0	0
Hdwd	0	0	0	4	Ч	3507	307	2	0	82	Ö	0	0	0	0
Pihd	2	0	Г	124	282	10	0	0	0	2	0	0	0	0	0
Pine	н	0	2	653	26	r-1	0	0	0	107	2	0	0	0	0
Crop	22	8	1402	0	0	н	2	0	0	36	0	0	0	0	0
Past	£	944	23	0	0	3.	0	0			0				
Soil	1855	2	6	Ч	0	0	0	0	0	147	ς	0	0	0	0
% Correct	95.3	92.6	97.0	81.1	89.8	87.7	85.1	98.9	0.0	86.3	97.6	99.2	100.0	97.4	100.0
No. of Pts.	1946	987	1445	805	314	3997	2242	350	35	4277	294	124	66	39	232
	Soil	Past	Crop	Pine	Pihd	Hdwd	Sghd	Tupe	Syca	Ccut	Mveg	Tuwa	Vege	Vеwa	Watr

Overall Classification Accuracy (15335/17153) = 89.4%

II. PROBLEMS ENCOUNTERED

No problems of significance were encountered during the past quarter. Some difficulties were encountered in following the methodology initially established for identification of the cover type in the defined test pixel, thereby causing some delay in the analysis of the 1979 TMS data. However, these problems have been resolved, and the modified methodology currently being used is much faster and should produce test data sets having a higher degree of reliability among the different analysts involved.

III. PERSONNEL STATUS

The following personnel committed the respective percentages of time to the project during the past quarter:

Name	Position	Ave. Monthly Effort_(%)
Bartolucci, Luis	Professional Research Analyst	10
Dean, Ellen	Research Associate	100
Frazee, Michael	Research Assistant	50
Hoffer, Roger	Principal Investigator	80
Knowlton, Douglas	Research Associate	50
Latty, Rick	Research Associate	100
Peterson, John	Associate Director	5
Prather, Brenda	Secretary	50
Stiles, Stephanie	Secretary	3

IV. ANTICIPATED ACCOMPLISHMENTS

The following are the anticipated accomplishments of the forthcoming quarter (September 1, 1980 - November 30, 1980):

- Digitization of the SAR data for Flight Line #1, HH and HV polarizations.
- 2) Completion of the definition of the test data sets for Study Site 1-N and 2-N.
- 3) Continuation of the analysis of the four different spatial resolutions of the 1979 data.
- Continuation of the analysis of the spectral characteristics of the 1979 TMS data.
- 5) Receipt of the 1980 TMS data and initiation of the reformatting and rectification procedures.

- 6) Prepare the 18-month report required by this contract.
- 7) Definition of the Statement-of-Work to be followed during F.Y. '81 and renegotiation of the contract for F.Y. '81.

No major technical problems are anticipated during the forthcoming quarter. Due to (a) an announced plan to significantly decrease the level of funding on this contract during F.Y. '81, and (b) the delays in obtaining, and characteristics of the TMS and SAR data obtained in support of this project, it is anticipated that the objectives initially proposed will need to be modified. These modifications will be reflected in the Statement-of-Work which will be developed during this next quarter.

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APPENDIX A

Paper entitled "Waveband Evaluation of Proposed Thematic Mapper in Forest Cover Classification," by R. S. Latty and R. M. Hoffer, to be presented at the 1980 Fall Technical Convention of the American Society of Photogrammetry, to be held in Niagara Falls, New York.

WAVEBAND EVALUATION OF PROPOSED THEMATIC MAPPER IN FOREST COVER CLASSIFICATION

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ABSTRACT

This study involved the evaluation of the characteristics of multispectral scanner data relative to forest cover type mapping, using NASA'S NS-001 multispectral scanner to simulate the proposed Thematic Mapper (TM). The objectives were to determine: (1) the optimum number of wavebands to utilize in computer classifications of TM data; (2) which channel combinations provide the highest expected classification accuracy; and (3) the relative merit of each channel in the context of the cover classes examined. Transformed divergence was used as a measure of statistical distance between spectral class densities associated with each of twelve cover classes. The maximum overall mean pair-wise transformed divergence was used as the basis for evaluating all possible waveband combinations available for use in computer-assisted forest cover classifications.

INTRODUCTION

Early work in leaf spectra analysis (Billings and Morris, 1951; Gates and Tantraporn, 1952; Gates, et al., 1965; Gausman, et al., 1969; Knipling, 1970; Wooley, 1971; Gausman, 1977) provided much of the initial understanding of the variations in the amount of radiant energy returned from vegetated surfaces. Colwell (1974) identified the value of hemispheric leaf reflectance as only one of several important parameters responsible for these variations, and cautioned against making inferences about scene reflectance from leaf spectra information alone. Plant canopy modeling efforts (Idso and De Wit, 1970; Nilson, 1971; Oliver and Smith, 1972; Suits, 1972; Colwell, 1973) have identified many of the parameters which account for variations in the amount of radiant energy returned from the scene. The selection of waveband combinations which will provide accurate classification of the various earth surface features requires an understanding of the reflective characteristics of those features relative to the various wavebands available. Properties of the data consequential to classification accuracy are not dependent solely on earth surface, atmospheric, and illumination conditions. They are also very dependent on the parameters of the sensor system to be employed (Silva, 1978). Therefore, the need exists to investigate these reflective properties employing data more closely simulating the data which will ultimately be employed for such classifications.

With parametric classifiers, the resulting classification accuracy is dependent on (1) the degree to which the

training classes (i.e., spectral classes) represent the spectral variability of their respective cover classes, and (2) the level of statistical "separability" among the training classes (Swain, 1978). The first condition is difficult if not impossible to assess without conducting the actual classification - the expense of which precludes evaluating many different waveband combinations. One can justifiably assume that the first condition is satisfied if the points providing the data for establishing the training classes are randomly generated, and are "sufficient" in number for each class relative to the number of wavebands employed. The number of samples statistically sufficient for the development of training classes increases exponentially with an increase in the number of channels employed in classifica-tion (Duda and Hart; 1973). Duda and Hart (1973) pointed out that, "beyond a certain point, the inclusion of additional features leads to worse rather than better performance." They provide an excellent review of the problem. This problem has also been examined by Allais (1966), Dynkin (1961), Fukunaga and Kessell (1971), Kanal and Chandrasekaran (1971) and others. The level of statistical "separability" can be computed from the mean vectors and covariance matrices associated with each of the training classes employing one of several statistical distance measures (Kailath, 1967; Swain, Robertson and Wacker, 1971; Wacker and Landgrebe, 1972; King and Swain, 1973).

METHODS AND ANALYSIS

Data Acquisition

The data were obtained on May 2, 1979 from the NASA NC-130 aircraft flying at an altitude of 20,000 ft. (MGD) over an area immediately south of Camden, South Carolina. The multispectral scanner (MSS) data were obtained by the NASA NS-001 multispectral scanner. (Table 1 shows the NS-001 scanner specifications as compared to the Thematic Mapper). Color and color infrared photographs (1:40,000 scale transparencies) were obtained at the same time. Cloud coverage was minimal and atmospheric conditions were considered excellent.

Data Handling and Preprocessing

The across track change in scale of the imagery was adequately reduced by employing a geometric model which describes the ground resolution element dimensions as a function of aircraft altitude, IFOV (instantaneous fieldof-view) of the scanner, and change in scan angle corresponding to the analog signal integration interval.

A study of the data quality revealed an apparent correlation between scan angle and response level (different for each channel). The relationships appeared to be sufficiently high to obscure sources of variation otherwise correlated with differences between cover classes. Therefore, an empirically derived function was generated which described the variation in response level by column (corresponding with scan angle). Data were employed from areas where no apparent stratification of cover class by column was present.* The shape of these functions were evaluated against both empirical (Anuta and Strahorn, 1973; Landgrebe, Beihl, and Simmons, 1977) and theoretical work (Kondratyev, 1969; Jurica and Murray, 1973) prior to actual response level adjustment. The final data product was considered appropriate for the analysis.

Table 1.	Comparison of the NASA NS-001 multispectral	scanner
• • • • • • •	and the proposed Thematic Mapper (TM).	

	NS-001	Hultispectral Sc	anner ⁽¹⁾	Proposed Thematic Happer ⁽²⁾				
Channel	Bandwidth (pm)	Low Level Input (W-CN ⁻² -SR ⁻¹)	NEAP	Channel	Bandwidth [µm]	Low Level input (W-CH ⁻² .SR ⁻¹)	×Eap	
1	0.45-0.52	8.7 x 10 ⁻⁶	0.5%	1	0.45-0.52	2.8 x 10 ⁻⁴	0.8%	
2	0.52-0.60	6.8 x 10 ⁻⁶	0.5%	2	0.52-0.60	2.4×10^{-4}	0.5%	
3	0.63-0.69	5.0 x 10 ⁻⁶	0.5%	3	0.63-0.69	1.3×10^{-4}	0.5%	
4	0.76-0.90	4.4 x 10 ⁻⁶	0.5%	•	0.76-0.90	1.6×10^{-4}	0.5%	
5	1.00-1.30	6.0 x 10 ⁻⁶	1.0%					
6	1.55-1.75	6.2 x 10 ⁻⁶	1.0%	5	1.55-1.75	8.0 x 10 ⁻⁵	1.01	
7(3)	2.08-2.35	4.7 x 10 ⁻⁵	2.06	6	2.08-2.35	5.0 x 10 ⁻⁵	2.41	
1	10.4-12.5	NA	NEAT=0.25°K	7	10.4-12.5	300 ⁰ K	NEAT=0.5 ⁰ K	

(1) Data was obtained from the "Operations Manual, NS-001 Hultispectral Scanner," NASA; JSC-12715, April 1977.

(2) Data was obtained from Salomonson, 1978.

(3) Channel 7 (2.08-2.35 µm) was not operational at the time of the mission; all subsequent references to "channel 7" refer to the 10.4-12.5 µm waveband.

Development of Spectral Classes A COMTAL Vision One/20, displaying a composite of channels 3, 4, and 5, in conjunction with the aerial photography, was employed to ascribe cover class labels and ground condition descriptions to line-column coordinates in the imagery in a supervised fashion. This approach was considered more appropriate than the unsupervised clustering approach, since cover classes could be defined more nearly independent of their spectral characteristics in the wavebands to be evaluated. The method used to develop training classes was of particular concern since the affect of different within-class variances for each channel by cover class on cluster class composition is not currently well understood (Bartolucci, 1978; Anuta, 1979). Once the training fields had been identified, they were grouped according to cover class. cover class groups of training fields were then individually clustered to resolve the cover classes into a set of spectral classes. This provided training class statistics correspond-ing to a set of spectral classes associated with each cover class. Clustering at this stage provided a means of

*The function was generated using data obtained outside of the area from which the data for this analysis was obtained. establishing the spectral classes on the basis of spectral variability within each cover class, but did not completely avoid the problem mentioned above. Failure to provide training statistics representing the spectral variability within each cover class was considered more deleterious to the objective of the study than clustering to obtain those classes.

Data Analysis

The mean vector and covariance matrix computed for each of the spectral classes define the individual statistical density associated with each respective spectral class. A measure of statistical distance between all pair-wise combinations of the spectral classes provides information on the "separability" of these spectral classes. This "separability" represents an <u>a priori</u> estimate of the probability of correct classification (Swain, Robertson, and Wacker, 1971) for measurements provided by each channel or channel combination. Only pairs of spectral classes belonging to different cover classes are of interest, since low separability between different spectral classes of the same cover class does not affect classification accuracy.

Transformed divergence was used to compute the separability. Divergence is defined as: $p_{-}(x)$

 $D = f[p_1(x) - p_2(x)] \text{ in } \frac{p_1(x)}{p_2(x)} dx$ (1)

or computationally, for the Gausian multivariate case: $D = \frac{1}{2} \text{ tr } [(\Sigma_1 - \Sigma_2)(\Sigma_1^{-1} - \Sigma_2^{-1})] + \frac{1}{2} \text{ tr } [(\Sigma_1^{-1} + \Sigma_2^{-1})(m_1 - m_2)] (m_1 - m_2)^T]$ (2)

> where: Σ is the covariance matrix and m is the mean vector associated with the respective spectral class, and

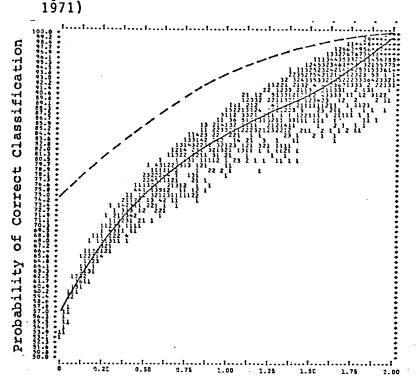
> > tr (trace) is the sum of the diagonal elements.

Since divergence increases without bound as the statistical distance between the two classes increases, a saturation transform is employed, resulting in a measure (i.e., transformed divergence) which corresponds more closely with percent correct classification (see Figure 1). After a certain level of statistical difference has been attained, virtually no confusion exists between the two class densities, and percent correct classification "saturates" toward 100%. The resulting transformed divergence is provided by:

$$TD = 2000 [1 - exp(-D/8)]$$
 (3)

There are some disadvantages to the use of transformed divergence as a measure of statistical difference between class densities*, but because of relative computational efficiency it is used in lieu of the alternative measures.

Figure 1. Probability of correct classification regressed against transformed divergence. (Swain et al.,



Transformed Divergence

Transformed divergence (TD) values were computed for each pair of spectral classes representing different cover classes, for each channel and channel combination. These mean pair-wise TD-values were then sorted for each set of combinations involving the same number of channels. The seven channel combinations providing the highest mean pairwise TD-values were obtained. Additional programs were written to generate summaries of the mean TD-values for each pair of cover classes (i.e., over all spectral classes representing the cover class pair) and each cover class

*It should be pointed out that transformed divergence is not "metric" in multivariate normal distribution functions of non-equivalent covariance matrices (Landgrebe and Wacker; 1972). That is, a pair of class densities having nonequivalent covariance matricies yet having equal mean vectors could have a transformed divergence value of zero. Also, there is no estimate for a lower confidence limit for the regression relation between transformed divergence and percent correct classification (Swain, Robertson, and Wacker; 1971).

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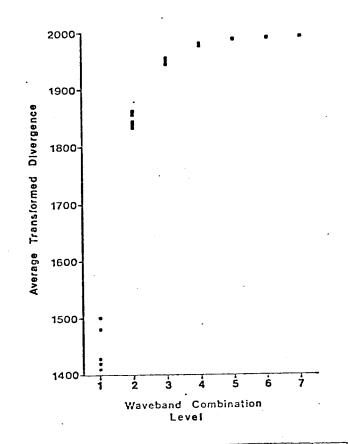
(i.e., over all cover class pairs involving the jth cover class; j = 1, ..., 12) for these seven channel combinations.

RESULTS AND DISCUSSION

To define the optimum number of channels to use in a classification, the relationship between cost of misclassification and the probability of error must be determined. Otherwise there is no meaningful way to compare classification cost to classification accuracy. It can be observed from Figure 2 that the increase in transformed divergence (the correlate to probability of correct classification) drops off sharply after three channels, and very little is gained by using more than four channels. This result is similar to those obtained previously with the Michigan M-7, 12-channel scanner (Coggeshall and Hoffer, 1973), and the skylab 13-channel S-192 scanner (Hoffer et al., 1975). The shape of the relationship shown in Fig. 2 indicates that transformed divergence increases logarithmically as the combination level increases linearly*. The spread of the points representing the five highest ranked channel combinations for each combination level represents the difference between



Averaged transformed divergence for the best five waveband combinations for each combination level.



*To simplify the following discussions, "combination level" will refer to the number of channels involved in any particular set of channel combinations.

successively ranked averaged transformed divergence. As seen in Fig. 2, the mean difference between successively ranked mean separabilities decreases logarithmically as the combination level increases linearly. This implies that the rank of overall mean separability as a feature selection criterion decreases in value as the number of features comprising the selected feature subset increases.

The best combined sources of information for distinguishing between various cover classes need not have as a subset the best single source of information. This is indicated in Table 2, which shows, for example, that the single channel having the highest mean TD-value (i.e., channel 6) is not included in the 2, 3, and 4 channel combination levels having the highest mean TD-values. By comparing Table 2 with Table 3, it can be observed that the best channel or channel combination for each combination level, on the basis of mean overall separability, is not necessarily superior on a per cover class basis.

Table 2. Channel combinations, ranked by overall mean TDvalue for combination levels one through six.

COMBINATION LEVEL

1	2	3	4	5	6
6	3,4	3,4,5	1,3,4,5	1,3,4,5,6	1,2,3,4,5,6
3	3,5	3,4,6	3,4,5,6	2,3,4,5,6	2,3,4,5,6,7
1	2,4	3,5,6	1,3,4,6	1,2,3,4,5	1,3,4,5,6,7
5	2,5	2,4,5	3,4,5,7	1,3,4,5,7	1,2,3,4,6,7
2	3,6	2,4,6	2,4,5,7	3,4,5,6,7	1,2,4,5,6,7
4	4,6	2,5,6	2,3,4,6	2,4,5,6,7	1,2,3,4,5,7
7	1,4	1,3,4	1,3,5,6	1,2,3,5,6	1,2,3,4,6,7

Table 3. Best channels and channel combinations by TDvalue for each cover class. TD-value is in parentheses.

COMBINATION LEVEL

	1	2	3	4
soil	3(1820)	24 (1941)	256(1987)	1346,2346,1356(1992)
past	6(1476)	35(1878)	345(1971)	3457(1987)
crop	3(1390)	34(1836)	345(1971)	1345(1991)
pine	2(1435)	34(1780)	346(1912)	3456(1960)
pihd	2(1580)	36(1883)	356(1982)	3456(1997)
hdwd	3(1688)	34(1881)	134(1933)	2346(1952)
sghđ	3(1691)	35(1933)	346(1960)	1345,1346,2346(1972)
tupe	6(1658)	34(1896)	245,345(1979)	2457 (1992)
syca	5(1753)	35(197 9)	345(1994)	1345,1346,1356(1999)
ccut	6 (1329)	46(1707)	356(1889)	3456(1947)
mveg	4 (1270)	14(1739)	134(1941)	1345(1990)
watr	5(1853)	25(1988)	246,256(1999)	1345,1346,1356(2000)

SOIL, bare soil; PAST, pasture; CROP, row and cereal crops; PINE, pine forest; PIHD, pine-hardwood mix; HDWD, old age hardwood; SGHD, second growth hardwood; TUPE, water tupelo; SYCA, sycamore hardwood; CCUT, clearcut areas; MVEG, marsh vegetation; WATR, river water and quarry water.

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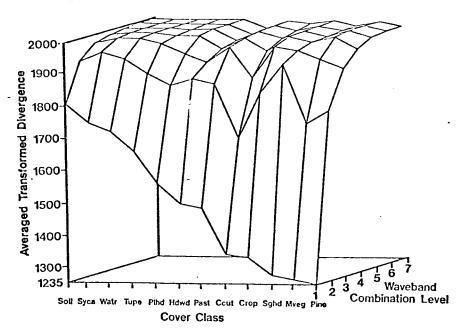
Examination of the transformed divergence averaged for each cover class pair indicated that the proper selection of a single channel may provide greater separability between two cover classes than a combination of two or three channels. More specifically, the channel combination with the highest mean separability for a particular combination level does not necessarily provide a greater separability for all cover class pairs than channel combinations of a lower combination level, when the combination of the lower level is not a subset of the combination of the higher level. Examples of this relationship are: soil vs. water has a mean TD-value of 1942 in channel 6 and a mean TD-value of 1824 in channel combination 3,4; PIHD vs. CCUT has a mean TD-value of 1835 in channel 6 and a mean TD-value of 1641 in channel combination 3,4; PINE vs. MVEG has a mean TD-value of 1424 in channel 1 (the channel ranked third on the basis of mean overall TD-value) and the mean TD-value of 1182 in channel combination 3,4 (the number one ranked channel combination of all combinations involving two channels). The same relationship holds for many other cover class pairs. Such a relationship was not found when the lower level channel combination was a subset of the higher level channel combination (as would be expected).

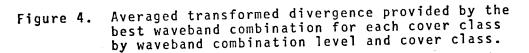
The additional average separability achieved for each cover class, by increasing the combination level, varies greatly between cover classes and combination levels, but generally decreases logarithmically with increasing combination level. Figure 3 can be thought of as a "separability response surface." The apparent length of the lines connecting different combination levels of the same cover class is proportional to the added separability resulting from the information in the additional channel. Note that the greatest increase in separability due to the addition of the second channel occurs with second growth hardwood. As one would expect, the smallest increase in separability occurs with that cover class with the highest single channel separability (soil, in this case). It should be noted that the lines connecting the different cover classes are present merely to indicate relative differences of separability and in no way imply any functional relationship.

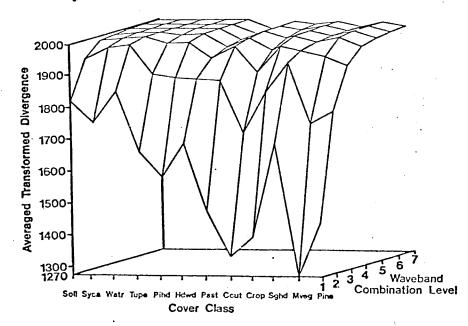
Figure 3 plots the maximum transformed divergence observed for each cover class in each combination level. This displays the maximum separability attainable for each cover class if the waveband combinations were selected on the basis of each cover class TD-value alone. As is clearly shown, the specific waveband combination resulting in each particular TD-value for any given waveband combination level is not constant over the different cover classes. In comparing Figures 3 and 4, it is apparent that the shapes of the curves increase in similarity with an increase in waveband combination level and are nearly identical in shape after combination level 4. This indicates that the separability by cover class provided by the best overall channel combination (Fig. 3) is nearly identical to the separability by cover class provided by the best channel combination for each individual cover class (Fig. 4) beyond waveband combination levels of 4. Thus, the best four waveband combination, based on overall transformed divergence, should provide very

close to the maximum classification accuracy for each individual cover type. However, if one were interested only in a particular cover type, high classification accuracy could be achieved using less than four channels of data.

Figure 3. Averaged transformed divergence provided by the overall best waveband combination by waveband combination level and cover class.







SUMMARY AND CONCLUSIONS

Based upon the results of this study, one would not expect a computer-based classification employing more than four channels to provide much improvement in classification accuracy. The highest overall mean separability was provided by channels 1, 3, 4, and 5 (0.45-0.52, 0.63-0.69, 0.76-0.90, and 1.0-1.3 μ m). This channel combination did not always provide the highest mean separability by cover class nor by pairs of cover classes. A different set of cover classes, or even a subset of the cover classes considered in this work, could result in other channel combinations yielding higher predicted classification accuracies.

Results such as these are highly data and application dependent. The conclusions pertain to channel subsets selected for classification and in no way imply that scanner systems need only obtain data in those channels in order to adequately provide remote sensory data to the various disciplines. Similar studies involving different cover classes and different seasons need to be conducted along with follow-up studies involving actual classifications.

ACKNOWLEDGEMENTS

This work was supported by NASA Contract NAS9-15889, NASA Johnson Space Center, Houston, Texas.

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Appendix B - Computer Programs Developed

The following is a list of some of the programs written during the quarter June 1, 1980 - August 31, 1980. A brief description is included to assist those in need of similar code.

- WGHT2 FORTRAN Reads a file containing: 1) number of the cover classes to which a spectral class belongs, and 2) the number of pixels from each spectral class. It then computes a weight for each spectral class pair and writes a disk file of "WEIGHTS" cards within the restrictions of *SEPARABILITY. Another disk file of real variable probabilities for the occurrence of each spectral class, and the conditional probability of the occurrence of the spectral class given the occurrence of the cover class of which it is a subset.
- GRID·FTN A FORTRAN program written for the PDP-11/34 to generate a user specified grid for use in systematic sample selection on the COMTAL Vision one/20.
- DIVPRT FORTRAN A modified version of the DIVPRT subroutine called in *SEPARABILITY which is the printer output supervisor. This was modified to write out the class symbols and separability for each channel combination and each channel combination level, for each spectral class pair.
- SPECSEP FORTRAN Reads the disk file created by the modified DIVPRT and computes the averaged transformed divergence by cover class pair. It also sorts for and prints out the minimum TD value.
- SUMG FORTRAN Reads the disk file created by the modified DIVPRT and computes the averaged transformed divergence by cover class (i.e., for each cover class over all cover class pairs - it uses the original TD_'s in order to avoid excessive rounding errors).
- CAGEN2 FORTRAN Reads a deck of COMTAL image coordinates and field descriptions; queries the user for the line-column coordinate of the first pixel displayed in terms of MIST coordinates; the run number desired on the output file; and pixel averaging if any. It then computes the MIST coordinates for each field and creates a disk file of LARS-12 card formatted records.

APPENDIX C

Tables of Averaged Transformed Divergence by Cover Class Pairs (generated by SPECSUP FORTRAN) and by cover Class (generated by SUMG FORTRAN).

Table C-1. Averaged and Minimum Transformed Divergence Values for Single Channels by Cover Class Pair.

			Cha	innels			
	6	<u>3</u>	<u>1</u>	5	2	<u>4</u>	<u>7</u>
SOCIOCOCOCOCOCOCOCOCOCOCOCOPP PP	163746672336020244120 1766773795020244120 11767723545693649142 11767111111111111111111111111111111111	197136779692 19738614579692 1186579692 11865879692	/0991630776436777641 189759725436777599725436777569725439972543997277545997277641 199621795997277641 199621 199621 199621	1196682815581961941705 19159858815581961999005 11198788281519655999005 1111111111111005	- 1000 - 475 - 508 - 1505 - 451	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1 - 1 - 1 / - 1 - 1 - 1 - 1 - 1 - 1 - 1

Table C-1. Averaged and Minimum Transformed Divergence Values for Single Channels by Cover Class Pair (cont'd.).

Channels

<u>6</u>	<u>3</u>	<u>1</u>	<u>5</u>	2	4	<u>7</u>
2160030020205372507539662366911149268801366615031666669076674091330091 122000600907482 1835221711302 593 354981226858 34399843435331756325277 12209009097482 1835221711302 593 354981226858 34399843435331756325277 122222 1 72215 22 603 112 44214 09358 29217453157215619351 122222 1 72215 22 603 112 44214 09358 29217453157215619351	910000000549272476288991060690320058274899302138848471753630091825 1 00000000488793084141684536435 499398191654466262344643619863719 87 1 2222221 11 11 11 11 11 11 11 11 11 11	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	790000802485845842245304060825628684111058511972450670578857984040 1 000009024858458422453040608256286841102435112754400500965242521017 1 222211151 1 641162433118 475475450670578857984040 1 22221217 1111 11 11 11 111111111	225521904992824100127248429049508623219699908690542685076039254083 80312707 5 60274 394577336895932097602868282980367782051313259035 1621 42 2 1 4 323137 3 3596 6 563 7 565930196994 3 111 11 11 11 11 11 11 11 11 11 11 11 11	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Table C-2. Averaged and Minimum Transformed Divergence Values for Each of Best 2-Channel Combinations by Cover Class Pair.

					<u> (</u>	Channe:	ls		
			3,4	<u>3,5</u>	<u>2,4</u>	<u>2,5</u>	<u>3,6</u>	4,6	<u>1,4</u>
SSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	TPEDDDEFATGRPEDDDEATGREDDDEATGRDDDEATGRDDEATGRDDEATGRDEATGRDEATGREATGRATGRATGRRF SONEWHPCUETONEWHPCUETNEWHPCUETENNEPCUETWEPCUETHPCUETPCUETCUETUETETT ARIIDGUYCVARIIDGUYCVAIIDGUYCVAIDGUYCVAGUYCVAGUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIIDGUYCVAIDGUYCVAGUYCVAUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIIDGUYCVADGUYCVAGUYCVAUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIIDGUYCVADGUYCVAGUYCVAUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIDGUYCVADGUYCVAGUYCVAUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIDGUYCVADGUYCVAGUYCVAUYCVAYCVAVAA ARIIDGUYCVARIIDGUYCVAIDGUYCVADGUYCVAGUYCVAUYCVAYCVAVAA	1300000053453860012495846526745135412015601090390805756022620290541 99000000952878599997979989999563468559489891049976888100639021407900148 990000009528785999979799899999563468559489891049976888100639021407900148 112222222211111111111111111111111111	95000000000000000000000000000000000000	520000000400341359024894764676591252393189540903940142700060005047999000000004003370652699332554423967333816979796704996909989078909900999992000000033706592755969332554423967333816979796704996909989078909900999999009991222222222222222222222	4400000705643369969520970491118076518991519620568860672808760290082 9800000905223330127480794271659774192793809400078970514803740390278 98000009052233330127480794271659774192793809400078970514803740390278	7000000004300480208974906568745678520193990550188530985704120480896 960000000237740055999394494899894194476952989905003964500245805460390159 96000000237740055999394494899894194476952989909970489890997907680790398 1222222211111111111111111111111111111	0740000081062282012559299831348300923691202683567034976984195900071 88900000085817927683484729962221433991659209683567034976989968999900277 88900000585817927683484729966222143399165920968356705989968999990277	1111222211111111111111111111111111111

<u>Channels</u>

<u>3,4</u>	<u>3,5</u>	2,4	2,5	3,6	4,6	<u>1,4</u>
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Averaged

				Ch	annels	<u>s</u>			
		A	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>	F	<u>G</u>	
>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	TPFODDEATGRPEDDDEATGREDDOEATGRODDEATGRDDDEATGRPEATGREATGREATGRATGRTGRGR SONHWHPOUETONHWHPOUETNHWHPOUETHWHPOUETWHPOUETHPOUETPOUETPOUETOUETCUETET AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOGUYOVADGUYOVAUYOVAYOVAOVAVA AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOGUYOVADGUYOVAGUYOVAUYOVAYOVAOVAVA AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOGUYOVADGUYOVAGUYOVAUYOVAYOVAOVAVA AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOGUYOVADGUYOVAUYOVAYOVAOVAVA AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOGUYOVADGUYOVAGUYOVAYOVAOVAVA AGIIDGUYOVARIIOGUYOVAHIDGUYOVAHOVA	14000000000000000000000000000000000000	580000003336400770099034099987184720777607005021819087090037070060 860000009099999098203507009897183599077990090090699800999999090050 99000000999999098203507009897183599077990090090699800999999090050	050000004229300730520190890617078104796050050328540889900739050069 9600000084998998006501908906170781047960509050328540889907590005080039 96000000849989980065049097050992050509408007056996037590005080039 912222221111111111111211211211211111111	190000009+25995658210442489620897176500450017017806081090869020084 9900000003782897459450498959820411994005900490189880742905790400079 9900000003782897459450498959820411994005900490189880742905790400079	72000000176337659766062979361099270620007046096865065780890040007 99000000999896999896999680738014180990207099038987066290877040029 91222222211111111111111111111111111	47000000235722457699014254535009010040990056083808058480140010079 970000009999899999899999888870299802708980899028996066590076060079 112222222111111111111111111111111211211	9600000020234552125565959887799368609198000020474094090087009049 94000000089979289641626949993856955479979909401799860984905380090999 11222222211111111111111111111111	
	>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	PFDDDDEATGRPEDDDFATGREDDDFEATGRDDDEATGRDDEATGRDFATGRDFATGREATGRTGRTGRTGRTGRTGRTGRTGRTGRTGRTGRTGRTGRT	994 994 994 994 994 994 994 994 994 994	9858 19960 1997 <	$ \begin{array}{c} \underline{A} & \underline{B} & \underline{C} \\ 9965 \\ 9966 \\ 9$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	<pre>VS PAGP 1991 1985 1990 1991 1987 VS PIHC 2000 2000 2000 2000 2000 2000 VS STUCE 2000 2000 2000 2000 2000 2000 VS STUCE 1996 1997 1997 1997 1997 VS PIHC 2000 2000 1997 1997 1997 VS PIHC 2000 2000 1997 1997 1997 VS STUCE 1996 1997 1997 1997 1997 VS VS VCUE 1996 1997 1997 1997 1997 VS SCUE 1997 1997 1997 1997 1997 1997 VS SCUE 1997 1997 1997 1997 1997 1997 VS SCUE 1997 1997 1997 1997 1997 1997 1997 VS SCUE 1999 1997 1997 1997 1997 1997 1997 199</pre>	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $

A	=	3,4,5
B.	=	3,4,5
С	=	3,5,6
D	=	2,4,5
E	=	2,4,6
F	=	2,5,6

G = 1, 3, 4

Table C-3. Averaged and Minimum Transformed Divergence Values for Each of Best 3-Channel Combinations by Cover Class Pair (cont'd.).

	<u>C</u>	hannels	<u>3</u>		
<u>A</u> <u>B</u>	<u>C</u>	D	E	F	<u>G</u>
$\begin{array}{c} 1451 \\ 139\\ 19965 \\ 19965 \\ 19965 \\ 19999 \\ 19999 \\ 19999 \\ 19999 \\ 19999 \\ 19999 \\ 19905 \\ 1205 \\ 1205 \\ 19975 \\ 1205 \\ 19975 \\ 120 \\ 19975 \\ 120 \\ 19975 \\ 120 \\ 19975 \\ 120 \\ 1997 \\ 120 \\ 199 \\ 1$	20000000034783334219348967618179736079793994894000 200000000347833342193489676181797360797949494000 200000000347833342193489679786997797360797949494000 2000000034783334219348967618111111111111111111111111111111111	1768 1999 2000 1228 1954	760000006123143655240602432919132590405890780942990901405690600990 890000000612314365524060243291913265904058907809429909 890000000769399773333606979502894779336596596590600990 1122222222111111111111111111111111111	$\begin{array}{l} 640000000911777780031701297350979344977095600070843110230404660200194\\ 930000000091177778003170129795097934497709560079909958088906739909940404000287\\ 93000000008942936059960047013800499734943069208800839790067399069404000287\\ 93000000009117777800317012939482994779996607990099098808890099404660200194\\ 1222222222111111111111111111111111111$	$\begin{array}{llllllllllllllllllllllllllllllllllll$

A = 3,4,5 B = 3,4,5 C = 3,5,6 D = 2,4,5 E = 2,4,6 F = 2,5,6G = 1,3,4 Table C-4. Averaged and Minimum Transformed Divergence Values for Each of Best 4-Channel Combinations by Cover Class Pair.

Channels	

					nannels	5		
		<u>A</u>	B	<u>C</u>	<u>D</u>	E	F	<u>G</u>
SSSSSSSSSPPEPPPPPPPPPPPPPPPPPPPPPPPPPP	PCPPESTSCM WCPPESTSCM WPPESTSCM WPFESTSCM WISTSCM WSTSCM WSCM WSCM WCM WWWW	460000000127930633034000008090015159720500055031359037700960000000 98000000057979099709800000909090599140500009907898909990094000000900 99000000057979790997098000000909090599140500009907898909990094000000900 99000000057979790997098000000909090599140500009907898909990094000000900 990000000579797909970980000009090905991405000099078989099900940000000900 9900000005797979099709800000090900905991405000009000090009000009000 990000000000	\$900000078438070605704000807994979005080000904499970091900028090999999999999999999999999999	910000000198980643089060007096048450053080808000203593806090046800000700 87000000048939999950880900009919088580230809007057909905940095900000800 99000000048939999950880900009919088580230809007057999909059400095900000800 9900000004893999999000009019088580230809007057999909059400095900000800 9900000004893999999000009019088580230809007057999900059400095900000800	600000006477909860130900080400471980501090760246570356005860600998 980000000568790999008090009057032589660409059008908068609999009999 990000005687909990090009057032589660409059008908068608068600999909999 990000000568790999009000905703258966040905900890806860806860099990900999	680000008409703140330396930760731475705000290836980640905150700309 99000000086969690999093099999037035499020400039099989807659989099909090909 9800000008696969099909309999900370354990204000390999898076599890999099090909 9800000008409703140330396999909005499020400039099989807659989099909909909909909 98000000084097031403303969307607314757050000290836988064090515070039990909009099009009090909009009009090000	2900000004068706590690590000930065609403000000379400321000360900609 9800000004994909990680890000093006560940800000008949079800019809000809 99000000049949099068089000009300656094080000000894907980099900900809 9900000004994909906808900000930065609408000000008949079800999000809 99000000004994909906808900000930065609408000000008949079800999000809 99000000004994909906808900000930065609408000000000000799999099009008009 9900000000049949009906890000009300656094080000000000000000000000000000000000	270600005379022340860100980830706302205040907999900990099990000409 990000000399449999990099009900900274009000090900704690900999900099990000909 9800000003994499999900900990090027400900000000000909000090900000909 9800000000

A	=	1,3,4,5
В	=	3,4,5,6
С	#	1,3,4,6
D	=	3,4,5,7
E	=	2,4,5,7
F	=	2,3,4,6

G =	1,	3,	5	,6	
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Table C-4. Averaged and Minimum Transformed Divergence Values for Each of Best 4-Channel Combinations by Cover Class Pair (cont'd.).

Minimum

		<u>C</u>	hannel	<u>s</u>		
<u>A</u>	B	<u>C</u>	<u>D</u>	E	<u>F</u>	<u>G</u>
6600000000120780117997080006097956785289080099904502602849060190000166 9900000007548907669780900080999956374969590077022999099430094890000899 1122222221111121111111212221211111111	$\frac{33000000046572088009958500094039178440759500000708064406467006690300185}{98000000006988299007499769800990579926507196000009011946003289084607000853}{9800000000699897909769895899009806293365507196000009011946003289084607000853}{9900000000000000000000000000000000000$	640000009200298710620700979150695007184020010186620481905410000986 99000000647399966401306009793708854073960903991902509089898909890000989 122222221111111111211212121111211112	$\begin{array}{l} 1300000007395408400490900970493988429697979830555630103809100500842\\ 990000000019459088890790900980079990459069699928005882605479093800800199\\ 990000000037738909990580900980079990459069699928005882605479098880800199\\ 9900000003773890999058090098007799045906999928005882605479098880800199\\ 99000000037738909900899007799045906498999880058826054790093800800199\\ 9000000003773890990089900779904590649899988005566301038809100500842\\ 990000000373954084004909009800779904590649899988005566301038809100500842\\ 990000000373954084004909009800779904590649899988005566301038809100500842\\ 990000000037395408400490900980007999045906498999880055663054790093800800199\\ 900000000000000000000000000000000$	560000001398806498490651460190843786100899170204160550701480600802 73000000013988064984906514601908437861008999730197690988909999090000 73000000013988064984590794012012178020797901976909889099990900000 73000000139880649849065146019084378610089997901976909889099990900000 730000001398806498490651460190843786100899979019760204160550701480600802	71000000019795904604301308007491973059039009908970500668809340700998 1950000000345189769013029090079925880390900099014986096290374090998 12222221111111111121121121121111111111	11222222221111111112112121211111121112

A	=	1,3,4,5
		3,4,5,6
С	-	1,3,4,6
D	=	3,4,5,7
Ε	н	2,4,5,7
		2,3,4,6
		1,3,5,6

Table C-5. Averaged and Minimum Transformed Divergence Values for Each of Best 5-Channel Combinations by Cover Class Pair.

			Channels							
			<u>A</u>	B	<u>C</u>	<u>D</u>	<u>E</u>	F	<u>G</u>	
SUSSESSESSESSESSESSESSESSESSESSESSESSESS	>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	POPPHSTSOM WOPPHSTSOM WPPHSTSOM WPHSTSOM WHSTSOM WTSOM W SOM WOMWMWW W ARTIDGUYOVARIIDGUYOVAIIOGUYOVAIOGUYOVAOGUYOVAGUYOVAUYOVAYOVAOGUYOVAAUYOVAAUYOVAAUAAAAAAAAAAAAAAAAAAAAA	\$4000000000000000000000000000000000000	9400000007075908700580900000050593708304000000890550948004660000809 99000000060989099002909000005908779086090000001805907999007999000909 990000000909099990029099000005908779086090000000180590799900979990000909 99000000090909999009900	70000000958890870051000000000000000000000000000000000	84000000079819099901500000909000087669600400097097889012200960000900 990000000799999099900000009060021599905090000990559919089700097000000900 990000009999999999900000009060021599906090009905559190897000970000000900 9900000099999999999	90000000906000999060000000000000000000	9500000020829045606209099705106465986060000000230090713902050500909 9900000009099990029099906508155045090000000190480797908990900909 99000000090999990290999065081550045090000000190480797908990900909 99000000090999990999009999065081550045090000000190480797908990900909 990000000090999990099990650815500450900000001904807979089909000909	62000000047835746902203000000604300021060000002701600720056900000009 99000000069999999999999999	

Α	=	1,	3,	4,	5,	6
B	=	2,	3,	4,	5,	6
С	=	1,	2,	3,	4,	5
D	=	1,	3,	,4 ,	5 ,	7
E	=	3,	,4 ,	,5 ,	6,	7
F	=	2,	,4,	,5,	6,	7
c	_	1	2	2	5	6

- A 1 2 4 5 6
- G = 1, 2, 3, 5, 6

Table C-5. Averaged and Minimum Transformed Divergence Values for Each of Best 5-Channel Combinations by Cover Class Pair (cont'd.).

		Ch	annels	<u>3</u>		
A	B	<u>C</u>	<u>D</u>	E	F	<u>G</u>
37 000000604380296011090000050042320339800000808684603620074900000487 9900000006043802960360900000500423207683076990000905298690066000939900000999 990000000809999087608609000000600768307699000009029969096909999000009999 99000000080999908760860900000600768307699000009029969096909999000009999 9900000008099990876086090000060076830088990000090299690968000999990000009999 9900000000809999087608609000006007683008899000009090299690000099990000009999	1949 1999	16000000985410279052090000099077890810900040075758000820076000000198 99000000076729087901309000000900749990820800090076909078500098000009999 9900000008999990099901309000000900749990820800009009090909099990000009999 9922222222	73000000036166021109809000505000693658010005703833705920062900000909 990000000197490999906609000908000795897908000980449790269099800090909 99000000019749099990660900090700718997709080009804497902690998000990900000909 12222222221111112111211211212121212121	00000008729904570790900000779779408408000090779490142804840200294 990000008729909999089000008799799409800000907794901428048402002999 990000008999990999908900000859938000009009009079968999008899 9900000008949999099990890000085993880000099029979088999008999 99000000087299004570790090000859938000009009079949014280480480000999999 9900000008729900457079009000007797794084080000090779490142804804804802000294	2000	$\begin{array}{l} 123232222111111111211211211211211211212122222$

A = 1,3,4,5,6 B = 2,3,4,5,6 C = 1,2,3,4,5 D = 1,3,4,5,7 E = 3,4,5,6,7 F = 2,4,5,6,7G = 1,2,3,5,6 Table C-6. Averaged and Minimum Transformed Divergence Values for Each of Best 6-Channel Combinations by Cover Class Pair.

					<u>Cł</u>	annels	<u>s</u>		
			<u>A</u>	B	<u>C</u>	D	E	F	<u>G</u>
SSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSSS	>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	PCPPHSTSOM VCPPHSTSOM WPPHSTSOM WPBTSTSOM WHSTSOM WTSOM WSOM WOM NY WW ARIIOGUYOVA9 IIOGUYOVAIIOGUYOVAIOGUYOVADGUYOVAGUYOVAUYOVAYOVAOVAVAA ARIIOGUYOVA9 IIOGUYOVAIIOGUYOVAIOGUYOVADGUYOVAGUYOVAUYOVAYOVAOVAVAA	960000007094008800A20000000000000000000000000000000	97 no oond 6 na 5 noodoon47 oo dooddag o 097 na b7 oor oo doodd 4 dwl awy 4 dd 678 no ddad oo 99 dooddadaa gaacaa a charaa aa	97.00000007096000006800000080002470310000000004707909990000000900 9900000000909900000099000000	860000000399150800065090000078056800450900000004079050077000000609 9900000008999990900006909000007905170027090000000079099090900009900 990000000999999010000690900000790517002709000000007909909090000900 9900000009999999010000690900000990900000000	97000000080910078008600090909070045000850000000001508906760097000000700 990000000809900990099009070097900670008700000000099990099000000900 990000000809900990	95000000000000000000000000000000000000	7600000037950070004300000000007790071001001007000000000045039050000075000000100 99000000037950009000059000000009900990090000000000

1,2,3,4,5,6
2,3,4,5,6,7
1,3,4,5,6,7
1,2,3,5,6,7
1,2,4,5,6,7
1,2,3,4,5,7

- G = 1, 2, 3, 4, 6, 7

Table C-6. Averaged and Minimum Transformed Divergence Values for Each of Best 6-Channel Combinations by Cover Class Pair (cont'd.).

		C	hannel	s		
<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>	<u>F</u>	<u>G</u>
300000000404780860009309000000005555009000800000066968059990088000000709 9800000000908490880908809000000900837,00950900000006696969078700999000000909 99000000080899909900079090000006009095550009000000000696969078700999000000909 990000000080899909900000000	370 0000006070907800000000000000000000000000	42000000010579067905300000000009655024090000905499070176008390000909 98000000009055990679053000000000096550240900000905499900999900999900 9900000009055990579053000000000009094990000090549990038200094900000909 99000000009055790579053000000000009655024090000090549990038200094900000909 990000000009057905790053000000000009655024090000090549990038200094900000909 990000000009057905790530000000000000965502409000009054999000999900094900000909 990000000000	62000000055553895700990009500027056590300700000007608400890088850000209 7700000003984898900097009099003805329080090000000770099089700888500000909 990000000398489890007909099900380532908009000000270099089700888500000909 99000000027909998489890079090999003805329080090000000770099089700888500000909	490000000094480750959090495029071790410900000000908408960059002007 97000000037999909909750730799087059020099099070570570590290099009007 97000000037999909750750730799087057057057057057059029009007 9700000000775999909750990990990870570570570590840099009007 97000000005705705990975099099087057057057059084009900900907 970000000000570590959009090000000000	440000000049267056006300000090090091490610600009000195805540071000000800 99000000059859099006800000008009529033090009009896908970099000000900 990000005985909900680000000080095290330900099009896908970099000000900 990000009999999900680000000009529033090900098969089700999000000900 90000009999999999990068000000009529003309090009900999000990000000000	45000000051989038007709000006007290430700000009903701810061900000100 990000000398790990028090000089013399033009000008709990896008999000009900 9222222222211111121122122230900000089013399033009000000870999089600899900000900 90000000000000000

A	=	1,2,3,4,5,6
		2,3,4,5,6,7
С	=	1,3,4,5,6,7
D	=	1,2,3,5,6,7
		1,2,4,5,6,7
		1,2,3,4,5,7
		1,2,3,4,6,7

Table C-7. Averaged and Minimum Transformed Divergence Values for the 7-Channel Combination by Cover Class Pair.

			<u>Ave</u> .	Min.
SUSSESSESSESSESSESSESSESSESSESSESSESSESS	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	PCPD FSTSOM WOPPHSTSCMWPPHSTSOM WPHSTSOM WHSTSOM WSTSOM WSCMWSCMWMWWWSCMUCACVACVACVALLER CONTRACTOR	0800000010970000000900000000000000000000	6500,00005013008900320000005008420036090000004203906866008500000900 99000000060970099009900090000000090096900990000000180299909999009900000900 990000000050130009900000000009009509900000000180299900999009900000900 990000000050130009900000000009009509900000000180299900999000000900 9900000000501300099000000000000000000000

Table C-8.	Average	Transformed	Divergence	Values	for	Each	Channel	by	Cover
	Class.								

Channels

	6	3	1	5	2	4	7
SOIL PAST PROPE PIHDD FUUCT SCUER WAT	1806 14726 13235 14265 14265 2937 126529 13252 13252 13252 13252	1820 1401 13972 13278 16969 1513 12261 12261 12261 1433	1730 13139 131496 13146 13567 15707 11608 11195 11608	146774 142774 1157223 11576523 11285 11285	$\begin{array}{c} 1771\\ 1331\\ 12350\\ 14380\\ 16008\\ 13097\\ 11075\\ 1075\\ 1495\end{array}$	119318 13938 11112 1428 1428 15759 11279 11279 11791	1558 1373 1074 1074 1179 9551 1257 1012

Table C-9. Average Transformed Divergence Values for Each of the Best Seven 2-Channel Combination by Cover Class.

Channels

	3,4	3,5	2,4	2,5	3,6	4,6	1,4
SPENEDODE SPENED	256003196276 9887853296876 1188986876 1188986876 11788785 118898676 11796276 11796776 1179777777777777777777777777	1934 1897 1793 1793 1937 1937 1997 1977 1977 19	1940 1920 17974 189974 18917 18972 189723 198735 199735	1977 55210568 1977 55210568 111111111111111111111111111111111111	1034130 103688175885 1168851758657 1168851758657 1168575	198776664 17786684778 177897087 1177897087	89752166555 204522196555 117788654679 79

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Table C-10. Averaged Transformed Divergence Values for Each of the Best Seven 3-Channel Combinations by Cover Class.

		(
	A	<u>B</u>	<u>C</u>	<u>D</u>	E	F	G	A = 3,4,5
SOIL	1977 1971	1978 1960	1980 1958	1940 1955	1984 1944	1987 1941	1975 1915	B = 3, 4, 5
CROP PINE PIHD	1971 1903 1947	1947 1912 1980	1941 1888 1982	1955 1895 1946	1925 1910 1979	1922 1996 1976	1914 1900 1955	C = 3,5,6
HÔHÔ S 3 HC	1919 1958	1929 1950	1925 1959	1913 1947	1915 1956	$1911 \\ 1949$	1933 1955	D = 2, 4, 5
TUPE SYCA CCUT	$1979 \\ 1994 \\ 1870$	1965 1990 1886	1957 1991 1839	$\frac{1979}{1974}$	1956 1971 1880	1947 1977 1885	$\frac{1940}{1988}\\1854$	E = 2, 4, 6
MVEG MATP	$1931 \\ 1995$	1885 1997	$ 1871 \\ 1996 $	1924 1997	1904 1995	$1903 \\ 1999$	$1941 \\ 1998$	F = 2, 5, 6
								G = 1, 3, 4

Table C-11. Averaged Transformed Divergence Values for Each of the Best Seven 4-Channel Combinations by Cover Class.

		(
	A	<u>B</u>	<u>C</u>	<u>D</u>	E	F	<u>G</u>	A = 1, 3, 4, 5
SOIL PAST	1991 1985	1990 1984	1992 1976		1991 1984	1992 1980	1992 1975	B = 3, 4, 5, 6
CROP PIHO PIHO FOUPFA STUPCA COVER WAT	1991 1951 1991 1948 1972 1991 1993 1993 1993 2000	1985 1960 1997 1947 1986 1986 1996 1997 1998	1983 1949 1989 1951 1972 1984 1999 1984 1999 1980 2000	1988 1931 1941 1970 1997 1997 1997 1997 1997	1986) 1980) 1980) 1980 19662 1	1979 1950 1952 1952 19739 19739 19733 1973 1973 1979	1931 1941 1999 1971 1975 1998 1938 1938 1938 1938 1938	C = 1,3,4,6
								D = 3, 4, 5, 7
								E = 2, 4, 5, 7
								F = 2, 3, 4, 6
								G = 1,3,5,6

Table C-12. Averaged Transformed Divergence Values for Each of the Best Seven 5-Channel Combinations by cover Class.

		(
	A	<u>B</u>	<u>C</u>	D	<u>E</u>	<u>F</u>	<u>G</u>	A = 1, 3, 4, 5, 6
SOIL	1995 1992	1996 1991	1995 1991	1997 1993	1996 1993	1995 1990	1995 1939	B = 2, 3, 4, 5, 6
CROP PINE	1995 1975	1993 1975	1993 1965 1993	1996 1962 1994	1995 1963 1998	1993 1969 1999	1988 1965 1996	C = 1, 2, 3, 4, 5
PIHD HDWD SGHD	1999 1961 1977	1999 1960 1976	1963 1980	1957 1977	1955	1954 1972	1964 1980	D = 1,3,4,5,7
TUPE SYCA CCUT	1995 1999 1969	1998 2	1999 2000 1962	1995 1999 1958) 1998 1972	1994 1998 1971	1998 1999 1962	E = 3, 4, 5, 6, 7
MVEG WATE	1997 2000	1994 2009	1997 2000	1995 2000	1987 1999	$1991 \\ 2000$	1995 2000	F = 2, 4, 5, 6, 7
								G = 1, 2, 3, 5, 6

Table C-13. Averaged Transformed Divergence Values for Each of the Best Seven 6-Channel Combinations by Cover Class.

		(Channe					
	A	B	<u>C</u>	D	<u>E</u>	F	<u>G</u>	A = 1, 2, 3, 4, 5, 6
SOIL PAST	1998 1995	1998 1995	1998 1996	1998 1995	1998 1994	1998 1995	1998 1994	B = 2, 3, 4, 5, 6, 7
CROP PINE PIHD	1995 1983 1999	$ \begin{array}{r} 1998 \\ 1980 \\ 1999 \end{array} $	1998 1979 1999	1996 1975 1997	1997 1974 2000	1996 1974 1996	1996 1975 1994	C = 1, 3, 4, 5, 6, 7
HDWD SGHD TUPE	1970 1932 1999	1967 1980 1997	1965 1980 1997	1970 1932 1999	1966 1980 1999	1968 1982 1999	1970 1983 1999	D = 1, 2, 3, 5, 6, 7
SYCA CCUT MVEG	2000 1980 1999	1999 1985 1996	2000 1983 1998	2000 1933 1997	2000 1982 1997	2000 1980 1998	2000 1981 1998	E = 1, 2, 4, 5, 6, 7
WATR	2000	5000 1990	2000	5000	2000	5000	2000	F = 1, 2, 3, 4, 5, 7
								G = 1, 2, 3, 4, 6, 7

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Table C-14. Averaged Transformed Divergence Values for the 7-Channel Combination by Cover Class.