

IMAGE ENHANCEMENT THROUGH DATA PROCESSING

by

T. E. Riemer

under the direction of

Prof. C. D. McGillem

INTRODUCTION

This work represents a continuation of that originated by Jack Derry and reported in LARS Information Note No. 052770: "A Preliminary Study of Image Quality Improvement Through Data Processing".

The basic problem considered was the reduction of the transient response "ring" produced by the sharp cutoff low-pass filter frequency response of the composite analog signal processing equipment employed in the recording and playing back of the airborne scanner data prior to digitizing and reformatting. This ring produces a train of "ghost" images each displaced in time and reduced in intensity compared to the preceeding image and overlaid on the original undistorted image. As shown in Fig. 1, this ring produces the multiple images or "ghosts" to the left of the road in the center of the photograph. It should be noted that the scanner movement with respect to time is from right to left.

In addition to reducing the optical quality of the scanner image, it is suspected that this transient ring may lead to data classification errors, particularly in regions immediately to the left of a discontinuity in luminance level. It should also be noted that any program which attempts to correct for variations in scene illumination resulting from cloud shadows must also correct for this transient ring which would occur at the cloud shadow boundaries.

DETERMINATION OF THE FREQUENCY RESPONSE OF THE COMPOSITE ANALOG SYSTEM

Since the distortion characteristics of each component in the analog signal chain are not available, it was decided to choose a signal of approximately 50% of the total dynamic range of the scanner data, assuming that distortion at this signal level is negligible, as a calibration reference signal to determine the composite analog system frequency response. In addition, this calibration signal must have been generated by a signal at the scanner output which can be described with reasonable accuracy by a minimum number of parameters, and must contain a sufficient data record length to include all significant oscillations of the transient ring without containing new data in the region of the ring. The calibration samples used by Derry from lines 701 to 705 and columns 340 to 390 of channel 5 of the color panels of Run 66005200, as shown in Fig. 2, seemed to match the desired criteria. It was assumed that the original analog signal at the scanner output for this area of the above run was composed of two rectangular pulses.

The basic approach used to determine an estimate of the frequency response of the composite analog system was to obtain the frequency spectrum for an average of lines 701 to 705 of the calibration samples, using the Fast Fourier Transform algorithm. FORT, choosing $N=1024$ so that a good approximation to the continuous spectrum is obtained, and dividing this spectrum by the frequency spectrum of the assumed rectangular-shaped input signal. Although this basic approach is fundamentally straight forward, a number of parameters had to be defined to obtain a good estimate of the system response.

Four parameters were chosen to describe the discrete estimate of each of the rectangular pulses assumed to have comprised the original analog scanner output signal for the calibration samples, which for the first rectangular pulse were defined as follows: the number of intermediate sample points between the "zero level" and the peak of the pulse (defining the leading edge of the pulse), defined as parameter N14; the number of sample points between the start of the record length of the data for the calibration area and the first data point on the peak of the first input pulse, defined as parameter N10; the number of sample points defining the duration of the peak of the pulse, defined as parameter N1; and the slope of the peak of the pulse, defined as DLTX1. The corresponding parameters for the second rectangular pulse were N27, N22, N28, and DLTX2.

Two criteria were used to determine the best set of parameters. First, since the discrete spectrum estimate of the frequency response of the analog system is defined as the ratio of the discrete frequency spectrum of the system output signal to that of the input signal for the chosen calibration sample, it is clear that if the poles and zeros of the numerator and denominator polynomials do not coincide at all frequencies, discontinuities will result in the frequency response estimate of the analog system. These discontinuities are clearly shown in Fig. 11 of Derry's report. If it is assumed that the frequency response of the composite analog system did not contain such discontinuities, which should be a reasonable assumption in view of the type of equipment employed, then the magnitude of the discontinuities in the resulting estimate of the system frequency response could be used as a measure of the accuracy of the parameters previously defined.

Second, if the estimate of the system impulse response is obtained from the inverse Fourier Transformation of the frequency components, two requirements must be satisfied. First, the impulse response must be casual; and second, the impulse response must decay essentially to zero after a finite time. After examination of the transient ring for many points in the run from which the calibration samples were chosen, it was found that the transient ring had significant values, greater than 0.5%, for the first 30 to 40 data points following the beginning of the transient.

After extensive analysis, the best parameter set for the assumed input signal was obtained. $N1=12$, $N10=1$, $N14=0$, $DLTX1=0.0$, $DLTX2=0.0$, $N27=0$, $N22=31$, $N28=12$, $PK1=92.0$, $PK2=-7.5$. Fig. 3, which shows the magnitude of the discrete estimate of the analog system frequency response, has discontinuities of at least an order of magnitude less than previously possible. Fig. 4 shows the corresponding discrete impulse response estimate of the composite analog system.

DETERMINATION OF THE DATA CORRECTION FUNCTION

The basic approach used to correct the data consisted of multiplying the frequency spectrum of a suitable impulse response correction function, based upon the estimate of the composite analog system impulse response, by the frequency spectrum of a line of uncorrected data.

Several criteria were used to determine a suitable impulse response correction function. First, ideally, the convolution of the composite analog system impulse response and the impulse response correction function should be a unit impulse. However, since the frequency spectrum of a unit impulse is a constant over the frequency range from zero to infinity, and since the composite analog system frequency response asymptotically approaches zero rapidly for normalized discrete frequency component estimates above about 230 as shown in Fig. 3, and since the spectral components of the

output of the composite analog system, being shaped by the frequency spectrum of the composite analog system, are significant only for normalized discrete frequency components below about 230, the frequency spectrum of the ideal impulse response correction function must be approaching infinity for components above 230. From a practical standpoint, such a function could not be used; since it would enhance any noise introduced by the tape or the digital processing of the uncorrected analog data which had normalized spectral components in the region above about 230 in Fig. 3.

Thus, it was necessary to consider a "shaping" function in the frequency domain which would "weight" that spectral region occupied by the uncorrected data; or another way to state the same criterion, the ratio of the frequency spectra of the desired impulse correction function to that of the composite analog system must be equal to the "shaping" function instead of unity. Since the impulse response of this "shaping" function must be as close to that of the unit impulse as possible, i.e., not having any significant secondary lobes, and must be described by a small number of parameters, the Hanning and Hamming "shaping" functions were considered. It should be noted that as far as this first criterion is concerned, the Hamming function is the best choice.

The second criterion, and possibly more important than the first, is that the impulse response of the correction function decay as rapidly as possible. The significance of the criterion lies in the fact that if an error is made concerning the data which immediately preceded the first data sample to be corrected, an oscillatory error will result in the "corrected" data having a magnitude proportional to the impulse response of the data correction function. Thus, if the impulse response of the correction function takes a long time to decay to insignificant levels, the "corrected" data will contain these oscillations which will propagate through the corrected data for approximately the same time duration as that of the impulse response of the correction function. Since spectrum analysis of numerous lines of uncorrected data indicated that significant components existed for about 236 discrete normalized components on a basis of 1024 total discrete spectral components, the Hanning frequency shaping function with a parameter of 236 produced a correction function with an impulse response which decayed in less than half the time required by the Hamming function.

The importance of the second criterion lies in the fact that the data points immediately preceding the first data point to be corrected on a given scanner line are lost because of the digitizing procedure employed during reformatting.

The third criterion for the impulse response correction function is that it must be causal. Thus, once a correction function is obtained which satisfies the second criterion, its impulse response is sufficiently delayed in time so that it approximates a causal response. The resulting function is shown in Fig. 5.

Before the spectral components of the data correction function are multiplied by those of a line of uncorrected data, one additional procedure must be considered. As a means of minimizing the correction error introduced by not knowing what preceded the first data point to be corrected, a ramp function beginning at the "dark level" calibration value and terminating 100 sample points later at the level of the first data point to be corrected was assumed to precede each line of uncorrected data. This ramp function is an approximation to the actual function produced during the time that the scanner mirror is partially covered by the scanner window, and its duration was approximated by examining line graphs of the digitized data before reformatting.

The effectiveness of this overall correction procedure is demonstrated by comparing Fig. 6 which represents a graph of the data on line 695 and Fig. 7 for line 705 of run 66005200 channel 5 to Fig. 8 and 9 respectively.

Conclusions:

Fig. 10 shows the results of the correction applied to the data of Fig. 1. More work is still required to obtain a better estimate of the original analog system impulse, or equivalently, frequency response characteristics upon which the data transient correction function is based. Much of the difficulty in obtaining a good correction function arises because of apparent analog system non-linearity and the limitations of the color panels as calibration standards.

Also, further work is necessary to determine if it is possible to generate a single correction function which would accurately correct all data channels and all runs made with the same basic analog recording equipment. Preliminary investigations have shown that the correction function generated from channel 5 of run 66005200 will correct the other channels of this run with essentially the same accuracy as was obtained for channel 5. In addition, this same correction function made an acceptable correction of the same channel and flight line taken 2 years later.

Although no classification of corrected data has been made to date, the necessary software exists; and it is felt that the present correction function would be suitable to perform an initial classification to determine the magnitude of accuracy improvement.



Figure 1. Scanner Image from Run 66005200, Lines 400-1000,
Columns 1-450, Channel 5.

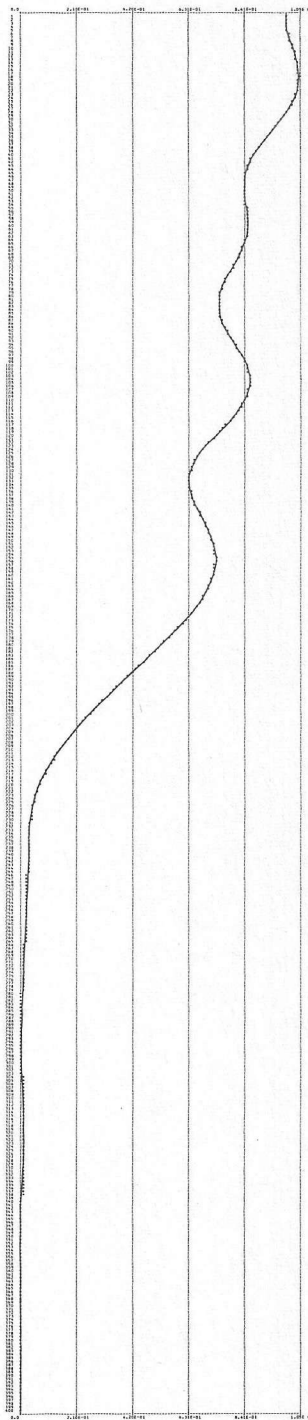


Figure 3. Frequency Response Estimate for Composite Analog System for Optimum Input Signal Parameter Set.

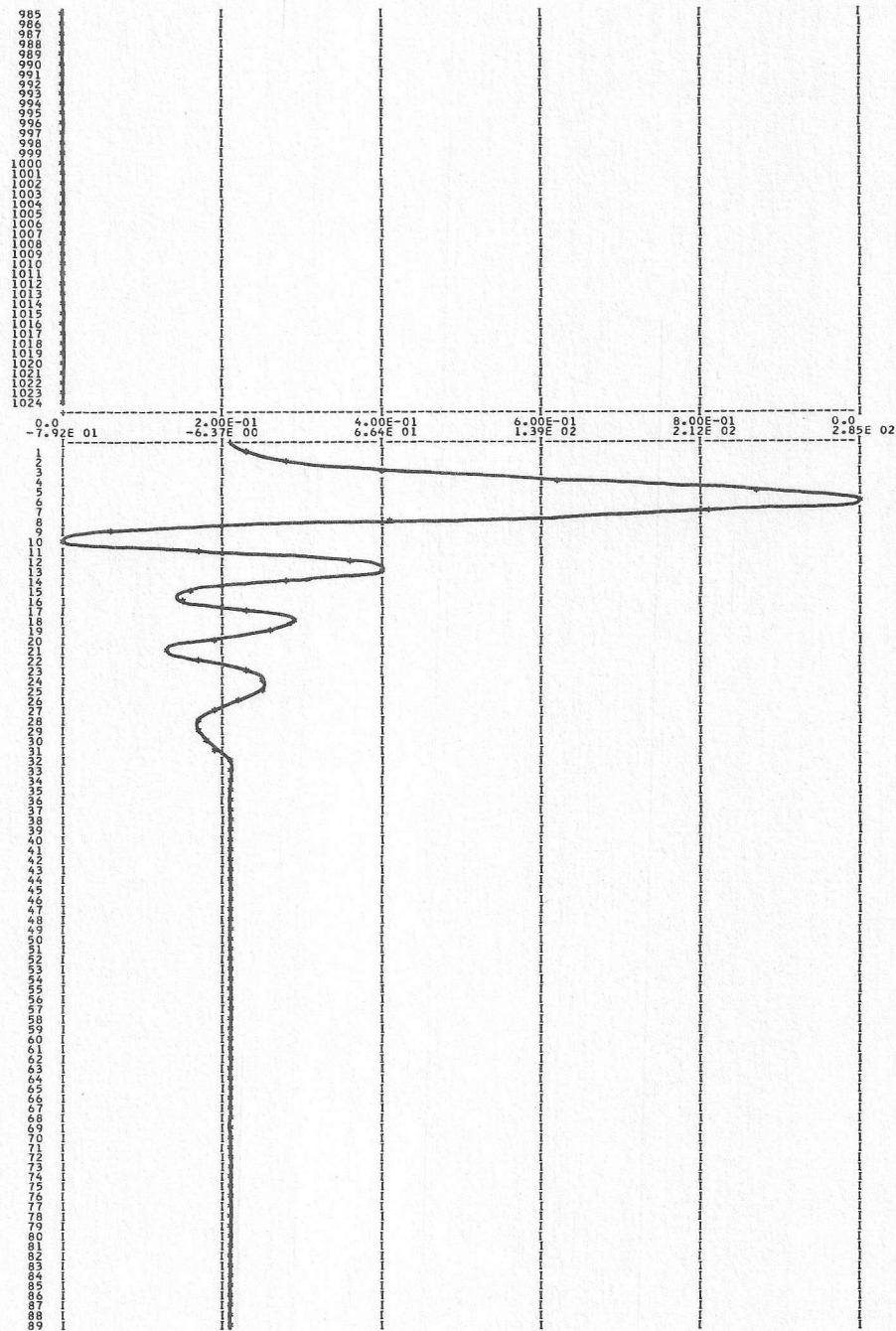


Figure 4. Estimate of Composite Analog System Impulse Response for Optimum Input Signal Parameter Set.

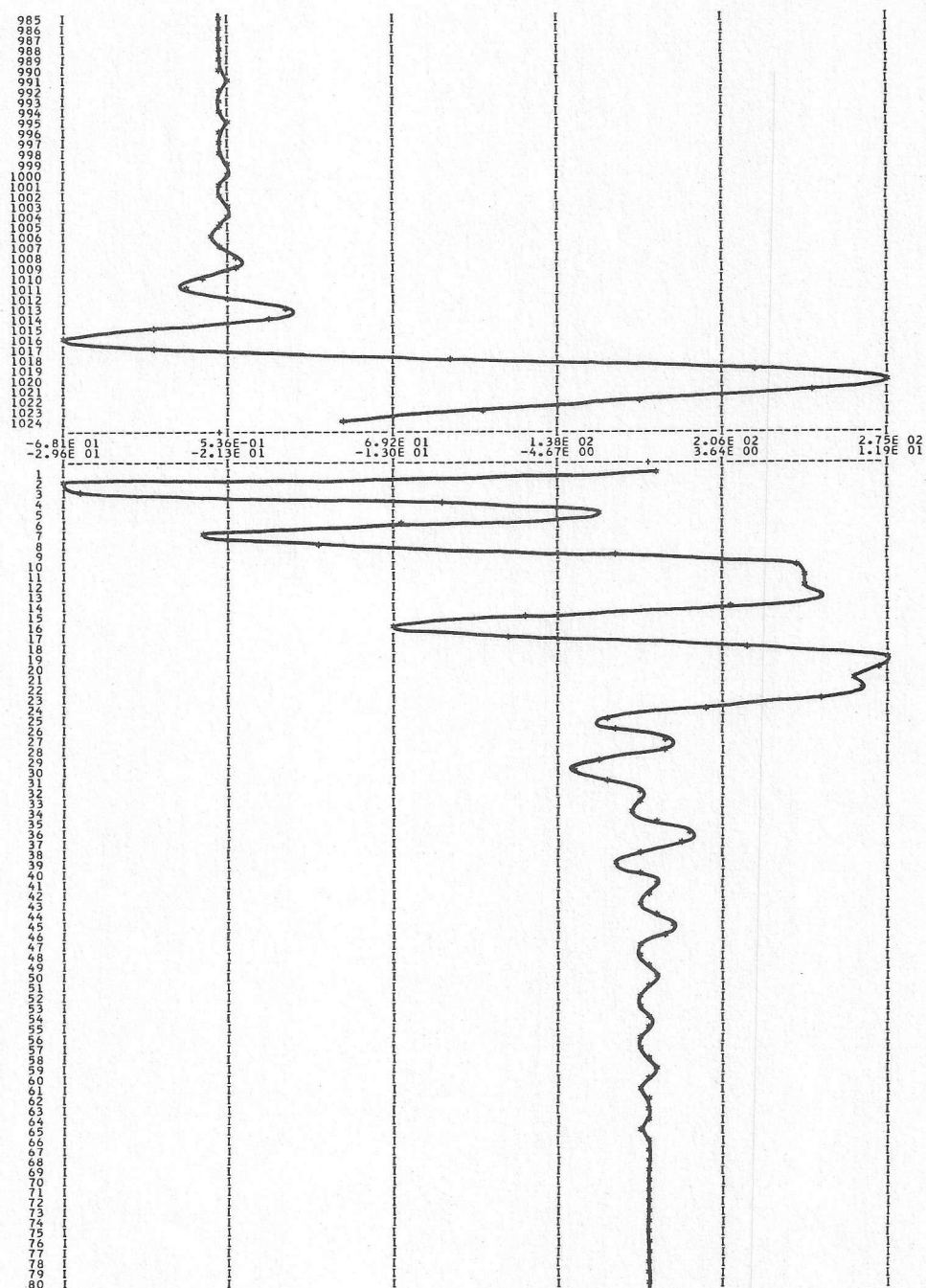


Figure 5. Impulse Response of Data Correction Function for a Hamming Frequency-Shaping Function of 236.

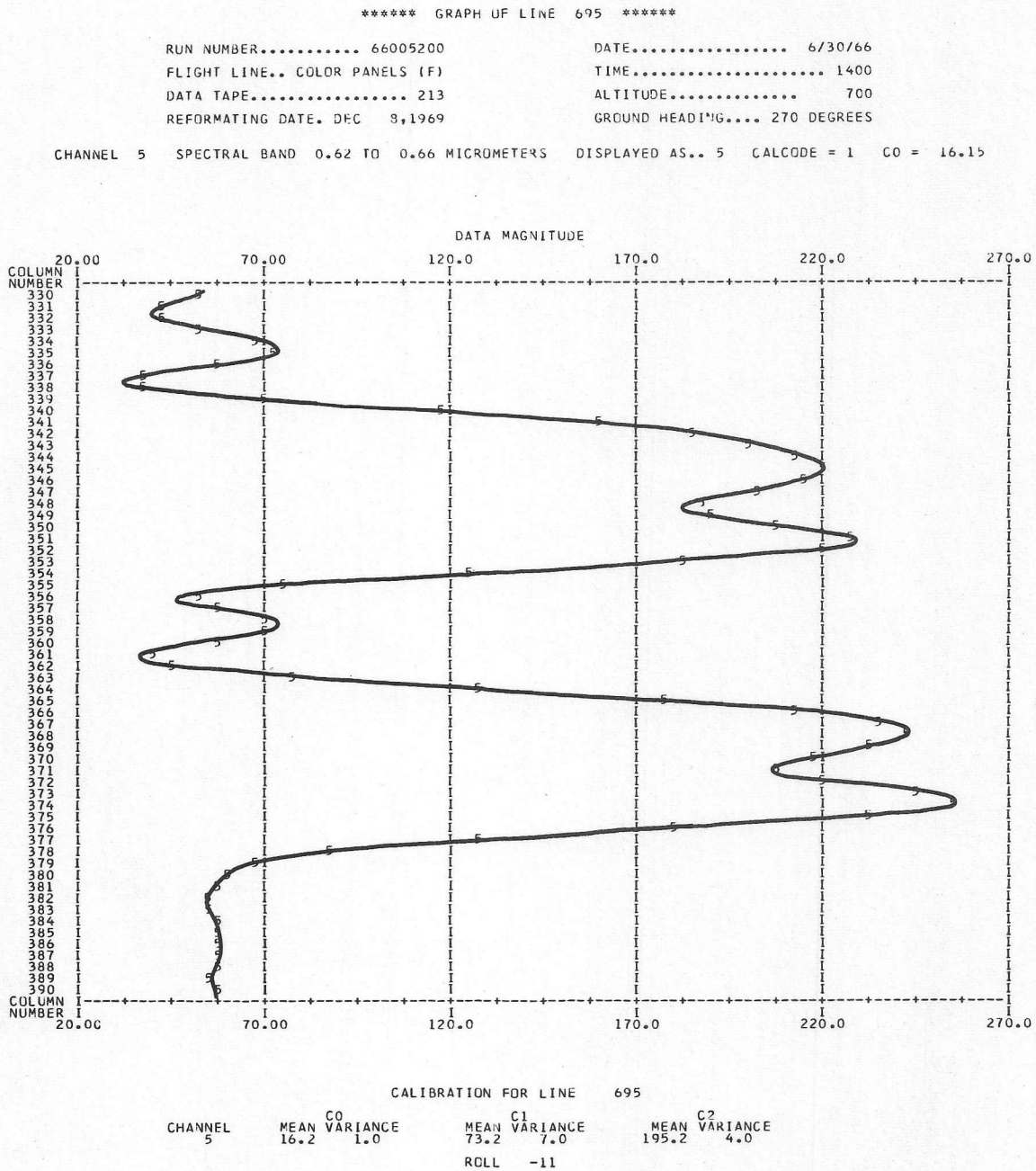
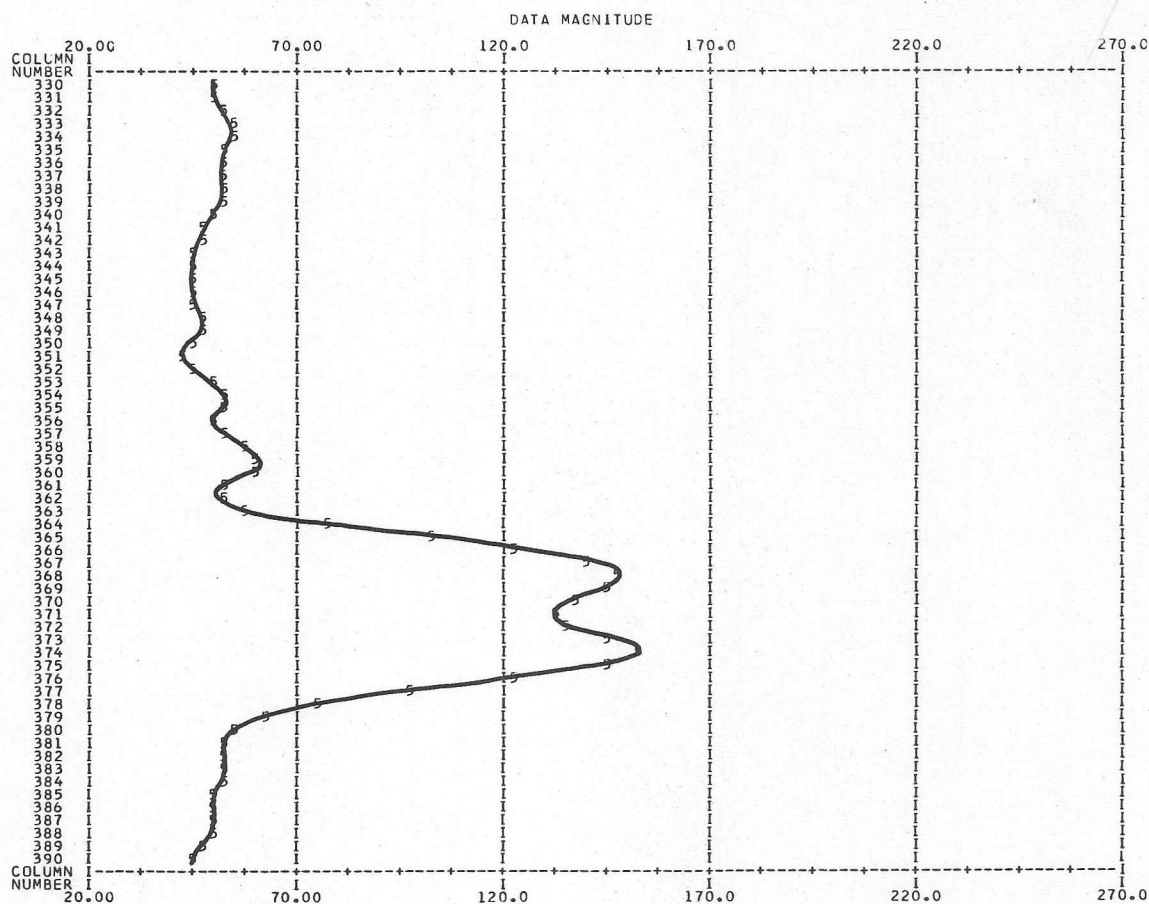


Figure 6. Graph of the Corrected Data in Line 695, Channel 5, Run 66005200.

***** GRAPH OF LINE 705 *****

RUN NUMBER..... 66005200	DATE..... 6/30/66
FLIGHT LINE.. COLCR PANELS (F)	TIME..... 1400
DATA TAPE..... 213	ALTITUDE..... 700
REFORMATING DATE. DEC 8, 1969	GROUND HEADING.... 270 DEGREES

CHANNEL 5 SPECTRAL BAND 0.62 TO 0.66 MICROMETERS DISPLAYED AS.. 5 CALCODE = 1 CO = 16.15



CALIBRATION FOR LINE 705

CHANNEL	MEAN	CO	VARIANCE	MEAN	C1	VARIANCE	MEAN	C2	VARIANCE
5	16.2		1.0	73.2		3.0	192.2		6.0
				ROLL		-12			

Figure 7. Graph of Uncorrected Data in Line 705, Channel 5, Run 66005200.

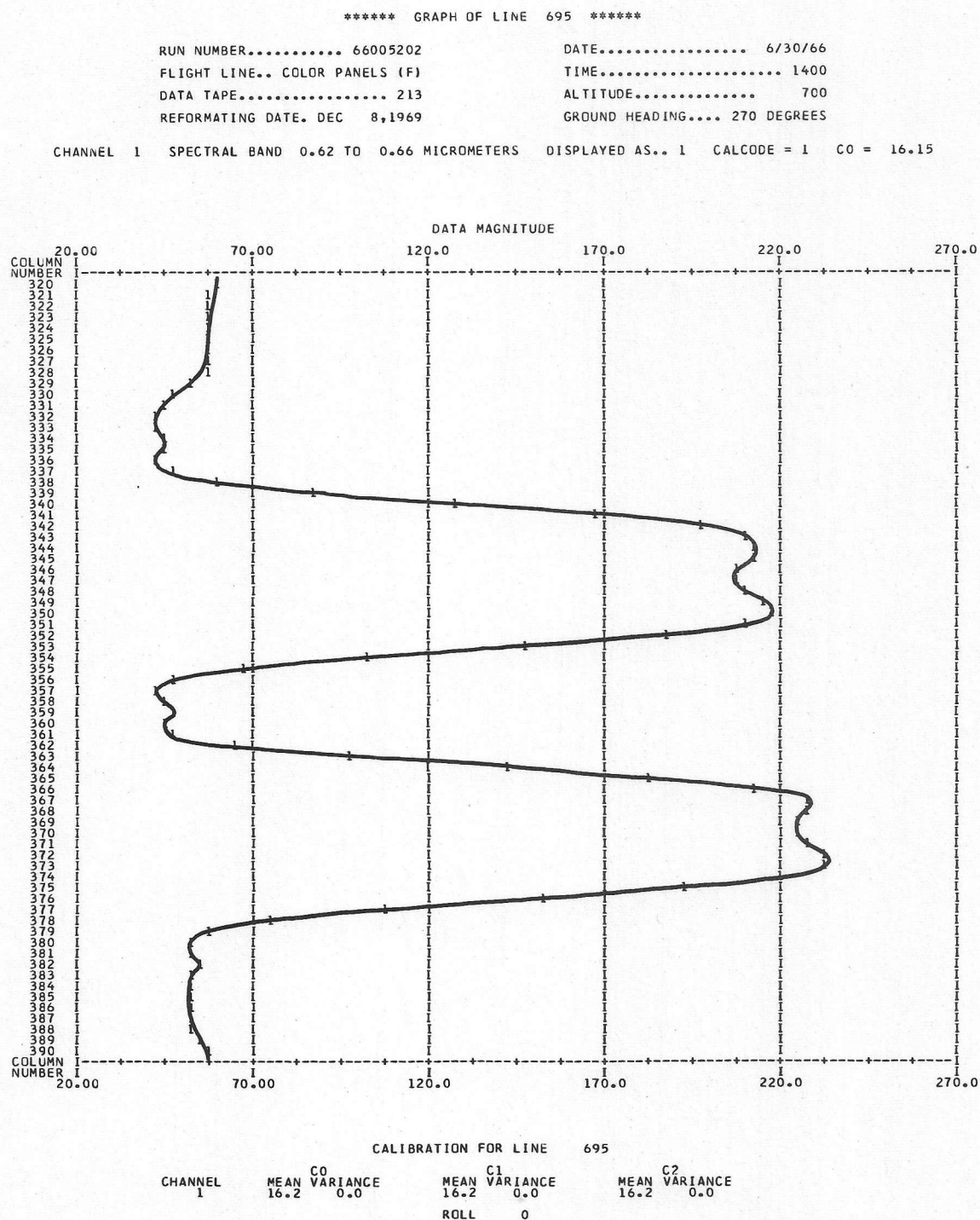


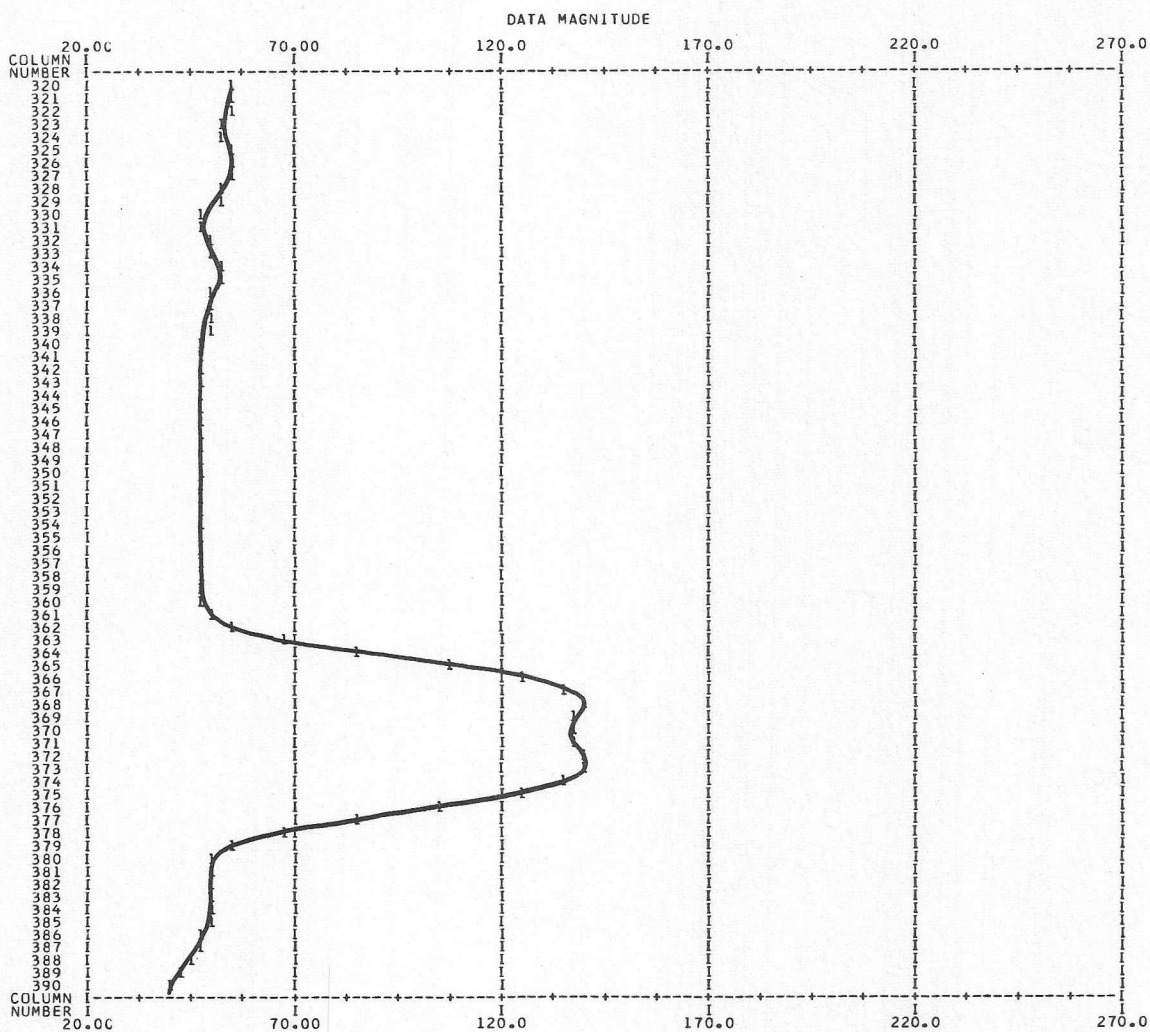
Figure 8. Graph of Corrected Data of Figure 6, Run 66005202.

***** GRAPH OF LINE 705 *****

RUN NUMBER..... 66005202
 FLIGHT LINE.. COLOR PANELS (F)
 DATA TAPE..... 213
 REFORMATING DATE. DEC 8,1969

DATE..... 6/30/66
 TIME..... 1400
 ALTITUDE..... 700
 GROUND HEADING.... 270 DEGREES

CHANNEL 1 SPECTRAL BAND 0.62 TO 0.66 MICROMETERS DISPLAYED AS.. 1 CALCODE = 1 CO = 16.15



CALIBRATION FOR LINE 705

CHANNEL	CO	MEAN	VARIANCE	C1	MEAN	VARIANCE	C2	MEAN	VARIANCE
1	16.2	16.2	0.0	16.2	16.2	0.0	16.2	16.2	0.0
				ROLL					
				0					

Figure 9. Graph of Corrected Data of Figure 7, Run 66005202.

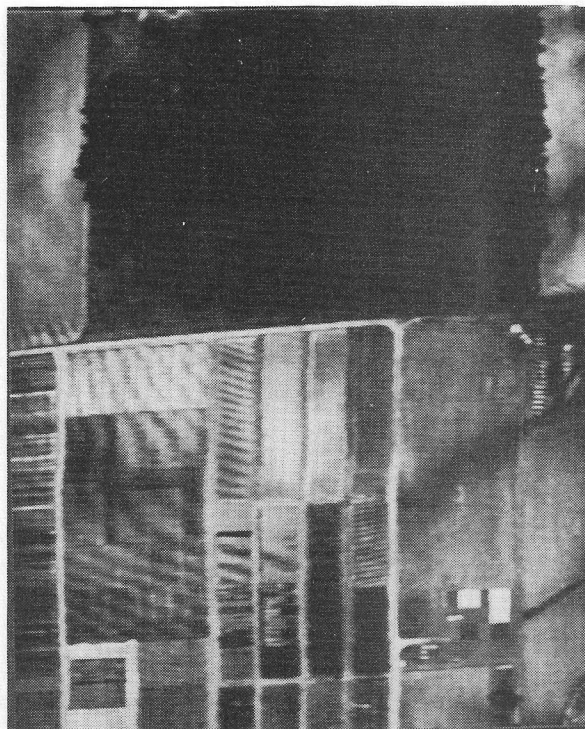


Figure 10. Scanner Image from Run 66005202, Lines 200--800,
Columns 1-450, Channel 1.

APPENDIX A:

The follow listing is a program used to compute analog system frequency and impulse response and correction function frequency and impulse response.

```

FORTRAN IV      MODEL 44 PS      VERSION 3, LEVEL 4      DATE 71143      PAGE 0001
C***** THIS PROGRAM COMPUTES HW AND HWL *****
C*****
0001      DIMENSION RY(100),X(1024),S(1024),X(1024),CH(1024),ICONT(13),
0002      1CH(1024),CH(1024),HAM2(1024),H(1024),CIN(1024),HAM(1024),
0003      DIMENSION TH(1024),CH(1024),H(1024),XC(1024),
0004      COMPLEX CY(1024),CH(1024),H(1024),XC(1024),
0005      COMPLEX HAM(1024),CH(1024),CH(1024),CH(1024),HAM(1024),
0006      INTEGER PUN
0007      ICONT(13)=1
0008      DO 9 I=2,12
0009          ICONT(I)=0
0010      9 ICONT(I)=0
C*****
0011      N1=NO OF DATA POINTS ON PULSE PEAK FOR PANEL 1
0012      N10= 1ST POINT ON FLAT TOP OF SQUARE WAVE FOR PANEL 1
0013      N14= NO OF INTERP POINTS BETWEEN MIN & MAX ON PANEL 1
0014      DLT1=CHANGE IN X OVER WIDTH OF N1 FOR PANEL 1
0015      DLT2=CHANGE IN X OVER WIDTH OF N28 FOR PANEL 2
0016      DLT2=NO OF INTERM POINTS BETWEEN MIN & MAX FOR PANEL 2
0017      N29=FIRST DATA POINT ON PANEL 2
0018      N28=NO OF DATA POINTS ON PEAK OF PANEL 2
0019      PK1=PEAK OF PANEL 1
0020      PK2=PEAK OF PANEL 2
0021      PK2=POSITIVE TIME DURATION OF INVERSE IMPULSE
0022      N29=1024
0023      NBC=TIME DURATION OF IMPULSE RESPONSE
0024      NBC=33
0025      NLW=240
0026      PUN=0 FOR NO PUNCHED OUTPUT
0027      PUN=1 FOR PUNCHED OUTPUT
C*****
0028      N=1024
0029      N2=N2
0030      N3=N1+1
0031      N4=N2+N1-1
0032      N5=N2+N1-1
0033      N6=N2+N1-1
0034      N7=N2+N1-1
0035      N8=N2+N1-1
0036      N9=N2+N1-1
0037      N10=N2+N1-1
0038      N11=N2+N1-1
0039      N12=N2+N1-1
0040      N13=N2+N1-1
0041      N14=N2+N1-1
0042      N15=N2+N1-1
0043      N16=N2+N1-1
0044      N17=N2+N1-1
0045      N18=N2+N1-1
0046      N19=N2+N1-1
0047      N20=N2+N1-1
0048      N21=N2+N1-1
0049      N22=N2+N1-1
0050      N23=N2+N1-1
0051      N24=N2+N1-1
0052      N25=N2+N1-1
0053      N26=N2+N1-1
0054      N27=N2+N1-1
0055      N28=N2+N1-1
0056      N29=N2+N1-1
0057      N30=N2+N1-1
C*****
0058      A4=1-N10
0059      5 X(1)=PR1*(DLT1/B2)*A4
0060      N1=N1+N1
0061      IF(N1-1,N13) GO TO 26
0062      DO 25 I=N13,N17
0063          A4=1-N1
0064          B3=N14
0065      25 X(1)=X(N11)-(X(N11)/B3)*A5
0066      N18=N17
0067      N19=N22-N27-1
0068      IF(N22-LT,N19) GO TO 41
0069      DO 34 I=N18,N19
0070          X(1)=0.0
0071      34 N20=N19+1
0072      N21=N22-1
0073      IF(N20-LE,N21) GO TO 19
0074      DO 35 I=N20,N21
0075          A6=1-N19
0076      35 B4=N27+1
0077      19 DO 36 I=N22,N23
0078          A3=1-N22
0079      36 X(1)=PR2*(DLT2/B5)*A7
0080      N25=N24+N27-1
0081      IF(N25-LT,N24) GO TO 38
0082      DO 37 I=N24,N25
0083          A8=1-N23
0084      37 B6=N27+1
0085      38 N26=N24+1
0086      GO TO 42
0087      41 N26=N18
0088      DO 4 I=N26,N
0089          X(1)=0.0
0090      4 X(1)=0.0
0091      6 C(1)=C(1)+X(1),0.0
0092      CALL FOR(C,M,S,-1,JACK)
0093      DO 16 I=1,N2
0094      16 HAM(1)=0.54+0.46*COS(A*P1)
0095      DO 17 I=N5,N
0096      17 HAM(1)=HAM1(N6)
0097      DO 18 I=1,N
0098      18 CH(1)=CY(1)/CX(1)*HAM1(1)
0099      CALL FOR(C,M,S,-1,JACK)
0100      NBC1=NBC-1
0101      DO 19 I=1,NBC
0102      19 HAM2(1)=1.0
0103      IF(NBC1-LE,N) GO TO 51
0104      DO 20 I=NBC1,N
0105      20 HAM2(1)=0.0
0106      51 DO 22 I=0.0
0107      12 CH(1)=REAL(CH(1))*HAM2(1)
0108      DO 14 I=1,N
0109      14 CH(1)=CH(1)*CH(1),0.0
0110      CALL FOR(C,M,S,-1,JACK)
0111      DO 47 I=1,N
0112      47 CH(1)=CH(1)/CH(1)
0113      DO 15 I=1,N
0114      15 CH(1)=C(1)+X(1)
0115      B=NLW
0116      P2=1.4159/B
0117      NLW2=N-NLW+1
0118      NLW3=NLW2-1
0119      NLW4=NLW1
0120      DO 27 I=1,NLW
0121      27 HAM3(1)=0.50+0.50*COS(A*P2)
0122      DO 28 I=NLW2,N
0123      28 HAM3(1)=HAM3(N6)
0124      DO 29 I=NLW3,NLW3
0125      29 HAM3(1)=0.0
0126      C1=0.0
0127      DO 30 I=1,N
0128      30 I=1,N

```

(Appendix A: Continued)

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0136 IF(CABS(CHC(1))-LT,C1) CHC(1)=CMPLX(C1,C1)
0137 C1H(1)=HAMS(1)/CHC(1)
0138 C1HM(1)=CABS(C1H(1))
0139 C1H(1)=C1H(1)
0140 CALL FORT(C1H,M,S,1,JACK)
0141 DO 31 I=1,N
0142 31 H(1)=REAL(C1H(1))
0143 31 H(1)=H(1)
0144 DO 39 I=1,N29
0145 39 TH(1)=H(1)
0146 DO 43 I=1,N
0147 40 TH(1)=0.0
0148 DO 43 I=1,N
0149 43 C1H(1)=CMPLX(TH(1),0.0)
0150 CALL FORT(C1H,M,S,1,JACK)
0151 DO 44 I=1,N
0152 44 C1H(1)=C1H(1)
0153 C1H(1)=CABS(C1H(1))
0154 H(1)=C1H(1)/C1H(1)
0155 CALL FORT(HM,M,S,1,JACK)
0156 DO 45 I=1,N
0157 45 HM(1)=REAL(HM(1))
0158 CALL FORT(HM,M,S,1,JACK)
0159 DO 32 I=1,N
0160 32 HAMS(1)=REAL(HAMS(1))
0161 DO 48 I=1,N
0162 48 XC(1)=C1H(1)/C1H(1)
0163 CALL FORT(XC,M,S,1,JACK)
0164 DO 49 I=1,N
0165 49 XC(1)=REAL(XC(1))
0166 N3=N3+24
0167 N4=N4+24
0168 8 CONTINUE
0169 WRITE(6,603)
0170 603 FORMAT(1H)
0171 WRITE(6,611) NCH
0172 611 FORMAT(5X,'CHANNEL NO ',I2)
0173 WRITE(6,607)
0174 607 FORMAT(95H 'SYSTEM RESPONSE
INVERSE RESPONSE ')
0175 1 WRITE(6,602) NO REAL MAG IMP RESP
0176 602 FORMAT(12H NO REAL MAG IMP RESP
REAL MAG IMP RESP )
0177 1 WRITE(6,604)
0178 604 FORMAT(1H)
0179 DO 10 I=1,N3,N4
0180 10 WRITE(6,601) I,CHC(1),C1H(1),CHC(1),C1H(1),C1H(1),H(1)
0181 601 FORMAT(15,1P2E13.4,1P2E13.4,1P2E13.4,1P2E13.4,1P2E13.4,1P2E13.4)
0182 WRITE(6,618)
0183 618 FORMAT(1H)
0184 WRITE(6,617) NCH
0185 617 FORMAT(5X,'CHANNEL NO ',I2)
0186 WRITE(6,618)
0187 618 FORMAT(25X,'TRUNCATED INVERSE RESPONSE')
0188 WRITE(6,619)
0189 619 FORMAT(4X,'DO',6X,'REAL',10X,'IMAG',9X,'MAG',6X,'IMP RESP',2X,
1'COMP IMP RESP',2X,'CORRECTED X')
0190 1 WRITE(6,620)
0191 620 FORMAT(1H)
0192 DO 46 I=1,N3,N4
0193 46 WRITE(6,621) I,C1H(1),C1H(1),TH(1),HM(1),XC(1)
0194 621 FORMAT(15,1P2E13.4,1P2E13.4,1P2E13.4,1P2E13.4,1P2E13.4)
0195 N3=N3+24
0196 N4=N4+24
0197 IF(N4-LE-N) GO TO 8
0198 50 WRITE(6,605)
0199 605 FORMAT(1H)
0200 CALL PLOTNR(C1H,ICONT,1,400,1)
0201 WRITE(6,606)
0202 606 FORMAT(1H)
0203 CALL PLOTNR(CHC,ICONT,924,N,1)
0204 CALL PLOTNR(CHC,ICONT,1,200,1)
0205 WRITE(6,608)
0206 608 FORMAT(1H)
0207 CALL PLOTNR(X,ICONT,1,60,1)
0208 WRITE(6,609)
0209 609 FORMAT(1H)
0210 CALL PLOTNR(C1H,ICONT,1,400,1)
```

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```
0211 1 WRITE(6,610)
0212 610 FORMAT(1H)
0213 CALL PLOTNR(HI,ICONT,924,N,1)
0214 CALL PLOTNR(HI,ICONT,1,200,1)
0215 WRITE(6,612)
0216 612 FORMAT(1H)
0217 CALL PLOTNR(HAMR,ICONT,974,N,1)
0218 CALL PLOTNR(HAMR,ICONT,1,50,1)
0219 WRITE(6,613)
0220 613 FORMAT(1H)
0221 CALL PLOTNR(TH,ICONT,974,N,1)
0222 CALL PLOTNR(TH,ICONT,1,200,1)
0223 WRITE(6,614)
0224 614 FORMAT(1H)
0225 CALL PLOTNR(C1H,ICONT,1,400,1)
0226 WRITE(6,615)
0227 615 FORMAT(1H)
0228 CALL PLOTNR(HM,ICONT,974,N,1)
0229 CALL PLOTNR(HM,ICONT,1,50,1)
0230 WRITE(6,622)
0231 622 FORMAT(1H)
0232 CALL PLOTNR(XC,ICONT,924,N,1)
0233 CALL PLOTNR(XC,ICONT,1,100,1)
0234 WRITE(6,623)
0235 623 FORMAT(1H)
0236 CALL PLOTNR(Y,ICONT,1,61,1)
0237 IF(PUS-EO-0) GO TO 33
0238 C DO 11 I=1,N2
0239 11 I=2*1
0240 11 WRITE(7,701) C1H(12),C1H(11),NCH,I
0241 701 FORMAT(4P2E13.4,1P2E13.4)
0242 C PLACE WRITE 7 STATEMENT CARD DO-LOOP BEFORE THIS CARD
0243 33 STOP
0244 END
```

APPENDIX B:

A program to correct digitized analog data.

[illegible]

(Appendix B: Continued)

```

10 I=J-KBDI+CHN-1+IDT(1,6)
20 IATA(I)=KDATA(J,CHN)
30 INIC=0
40 NID=1
50 OUTING=0
60 NOBYS=4
70 NCHAN=16
80 (OUTBY,NIDBYS=4
90 (DATA,INNOIS,INIC,JDATA,OUTDIS,OUTING,NOBYS)
100 JDATA(I)=NID
110 CALL TOPK(OUTUT,OUTTRY,ERR,JDATA)
120 IF (J=SE) INIC=JDO 100
130 BLOCK(I)=BLOCK(I)+1
140 GO TO 80
900 CALL TOPF(OUTUT,ERR)
1000 NID=NID+1
901 NID=NID
COUNT=800
CALL TOPK(OUTUT,COUNT,ERR,NID)
CALL TOPF(OUTUT,ERR)
CALL TOPF(OUTUT,ERR)
CALL TOPK(OUTUT)
CALL TOPK(UNIT)
STOP
END
// EXEC LNKED
// EXEC
9.9995751E-01 0.0000000E+00 9.99977595E-01 1.7190496E-02 5 1
9.9997751E-01 2.723703E-02 9.99977595E-01 1.7190496E-02 5 2
9.9997751E-01 2.723703E-02 9.99977595E-01 1.7190496E-02 5 3
9.9997751E-01 2.723703E-02 9.99977595E-01 1.7190496E-02 5 4
9.9997751E-01 2.723703E-02 9.99977595E-01 1.7190496E-02 5 5
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